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**COMSOL
CONFERENCE**
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3D Modeling of a Planar Discharge in a CO₂ Laser Using a Multilevel Approach

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... is one of the leading manufacturers of laser sources and laser-based solutions for industrial materials processing.



Macro

The Power of Light

- Hamburg/Germany
- High-powered industrial material processing

Micro

Focus on Fine Solutions

- Starnberg/Germany
- Laser sources and systems for processing materials down to the micro range

Marking

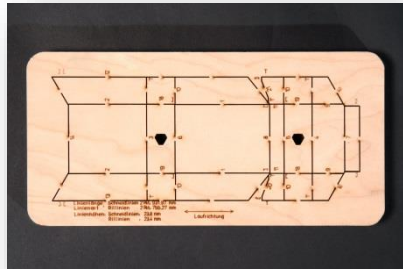
The Mark of Excellence

- Bergkirchen/Germany
- Marking solutions that consistently fulfill customer requirements in regards to precision, individuality and economic efficiency

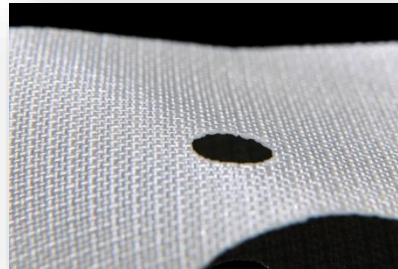


Application Examples

Cutting (Metal & Non-Metal)



Dieboards



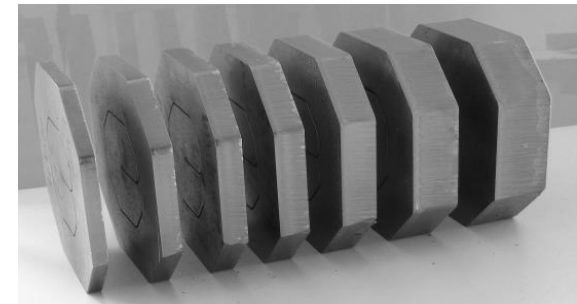
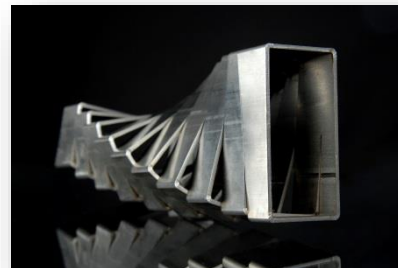
Airbag fabrics



Acrylic



Tableware



ROFIN Product Portfolio

Macro – The Power of Light

Fiber Lasers



CO₂ Lasers



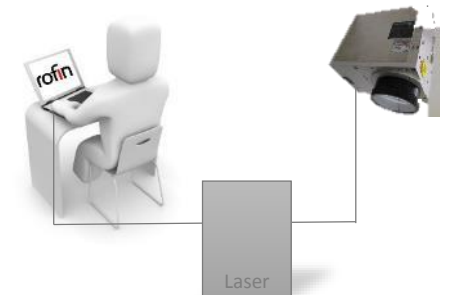
Diode Lasers



Solid-State Lasers

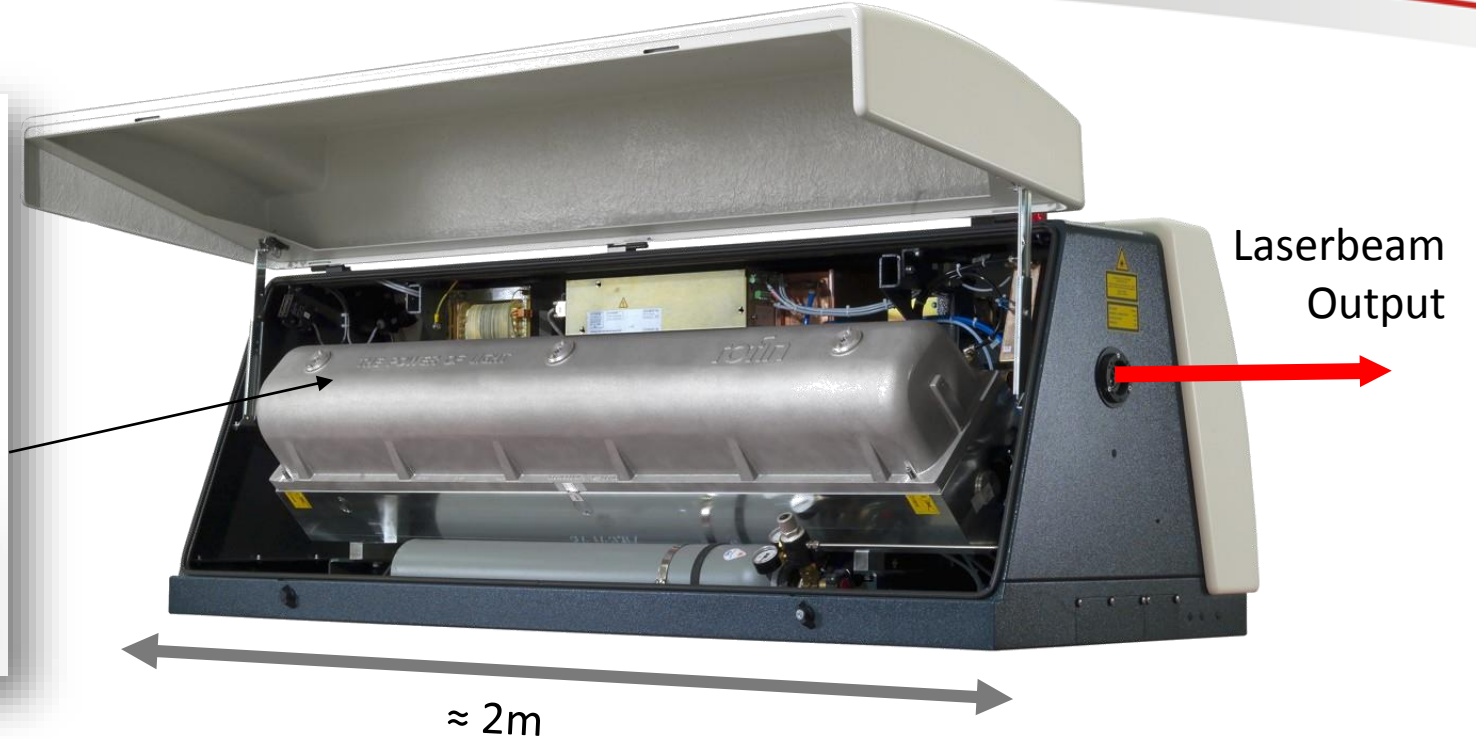


Laser Systems



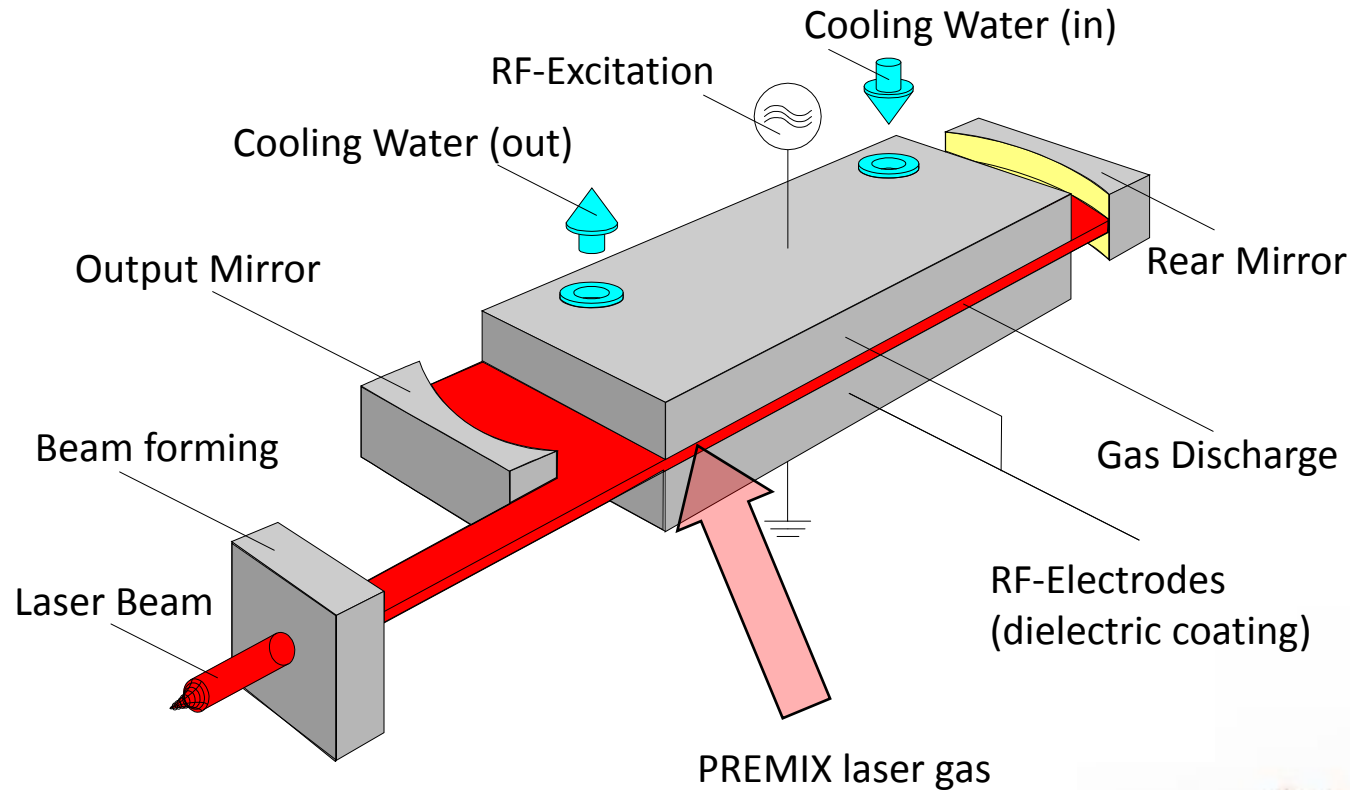
Slab laser principle

Laser head (resonator side)



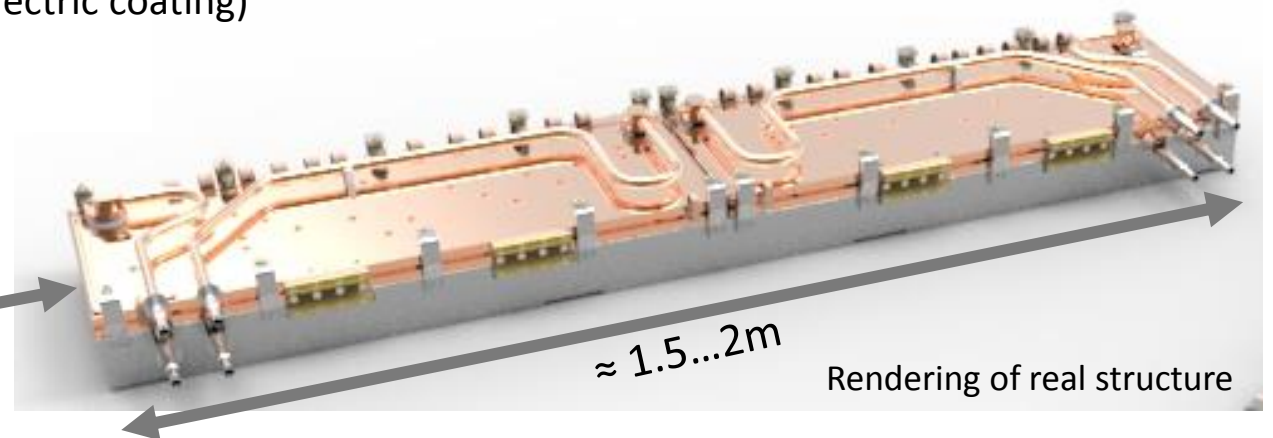
Slab laser principle

Resonator



- Real laser: complex 3D geometry only few symmetries
- Simplified geometry is not applicable for RF simulation
- **Advantage:** Plasma discharge region is almost perfectly „1D“

Electrode gap
 $\approx 1...2\text{mm}$

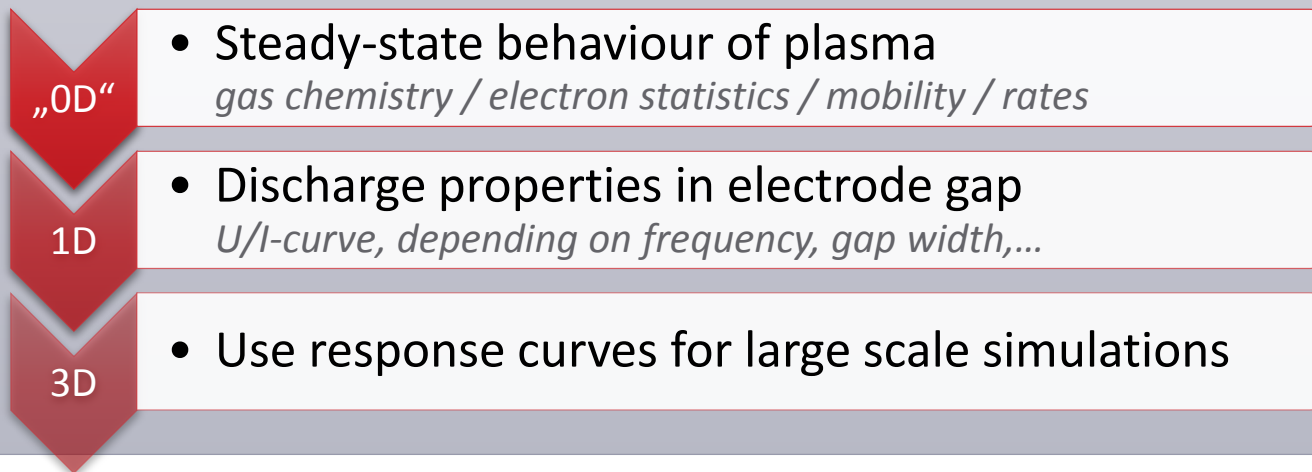


- Task: simulate homogeneity of discharge
- Direct 3D simulation of plasma \Leftrightarrow RF:
 - ▶ Huge span of time and length scales
 - ▶ Too many degrees of freedom
- Solution: separation of scales (+ dimensions)



μm \longleftrightarrow m
ns \longleftrightarrow s...h

Multi-level approach (*model hierarchy*)



Slab laser principle

Laser head (resonator side)



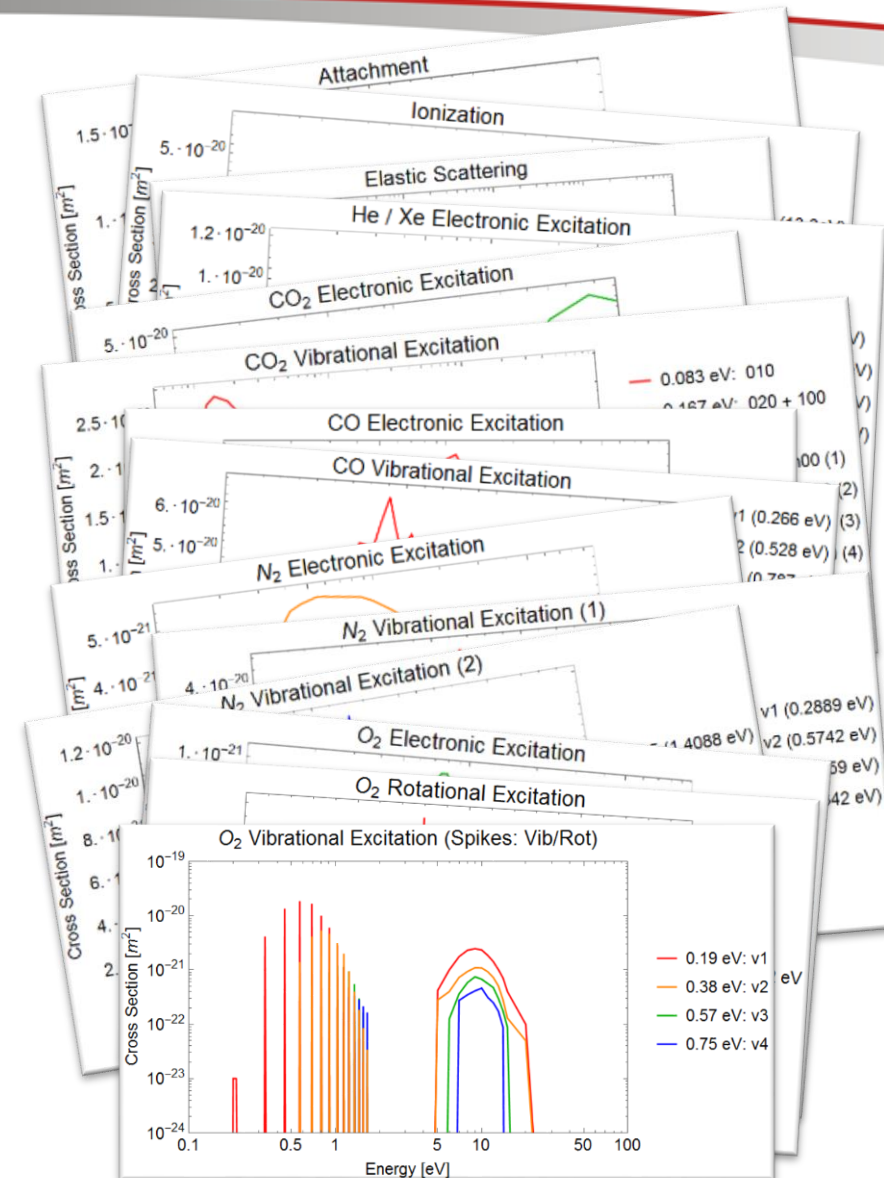
Integrated Gas Supply – PREMIX Gas Cylinder

Recipient bounds modeling domain
(no need for PML/TBC)

Lasermix® 690:
65% He, 19% N₂, 4% CO₂, 6% CO, 3% O₂, 3% Xe

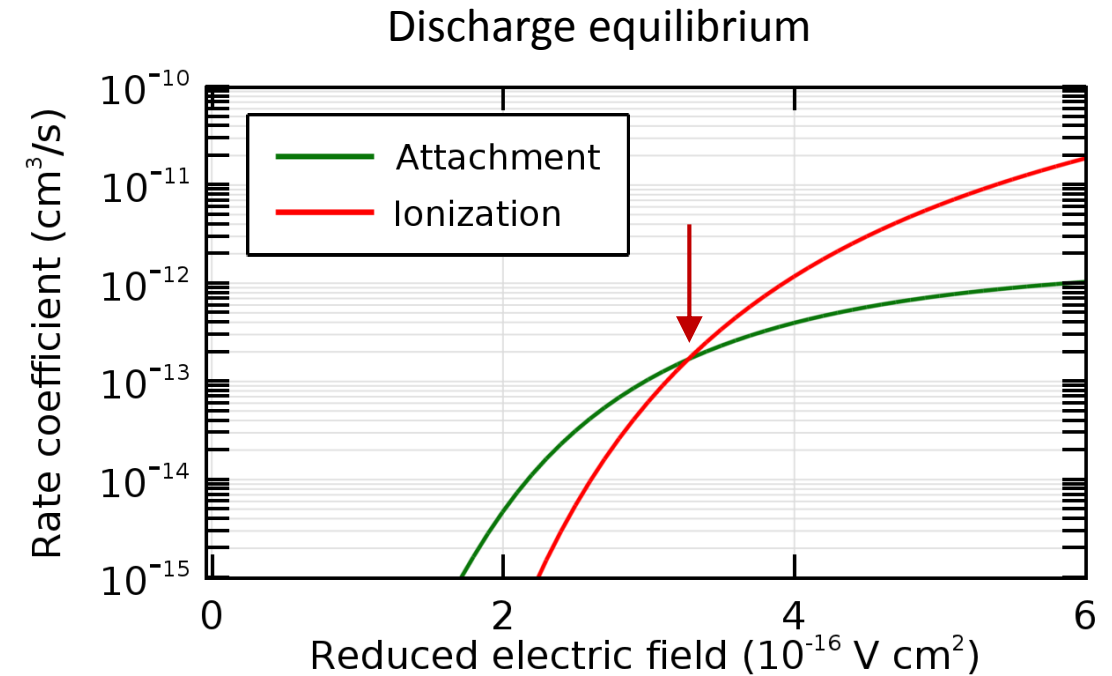
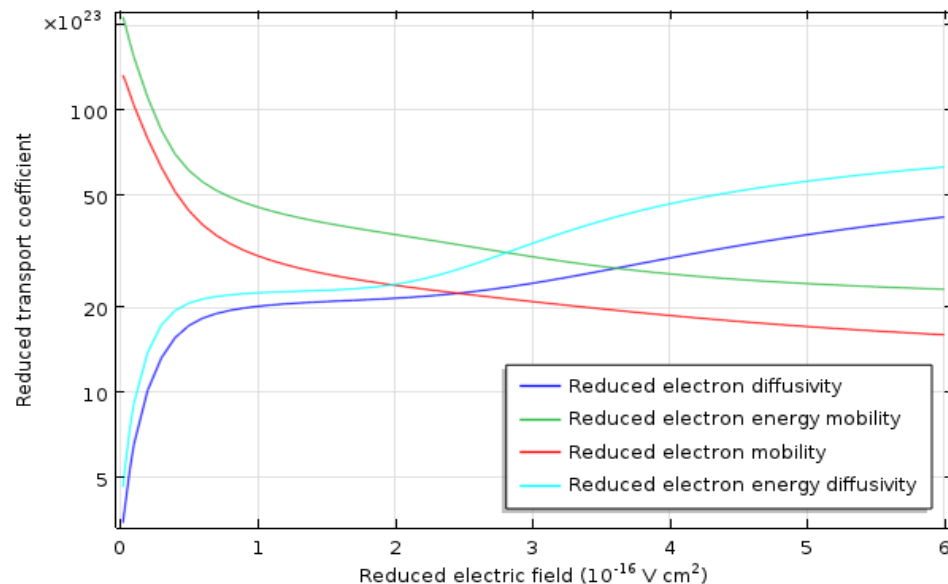
Lasermix® 690:

- 6 gas mixture components
(65% He, 19% N₂, 4% CO₂, 6% CO, 3% O₂, 3% Xe)
- 21 (relevant) molecule species
(plus vibrational levels)
- 59 relevant electron collision processes
- For each reaction:
effective collision cross sections ...



Step 1: Plasma Properties (0D)

- Electron energy distribution function (EEDF) not known a priori
- Calculation of EEDF, mobilities and rates (Boltzmann Equation, Two-Term Approximation)
- Interpolated functions for subsequent simulations



Step 1: EEDF + Rates (Results)

- Calculated rates agree with known roles of mixture components in the discharge:

He	cooling	Highest elastic contribution
Xe	ionization	Highest ionization rate
O ₂	attachment	Highest attachment rate in equilibrium
N ₂	energy transfer	High electron impact cross section (vibration)
CO ₂	laser transition	Resonant coupling to N ₂ vibration
CO	Long term stability	Dissociation equilibrium CO / CO ₂ / O ₂

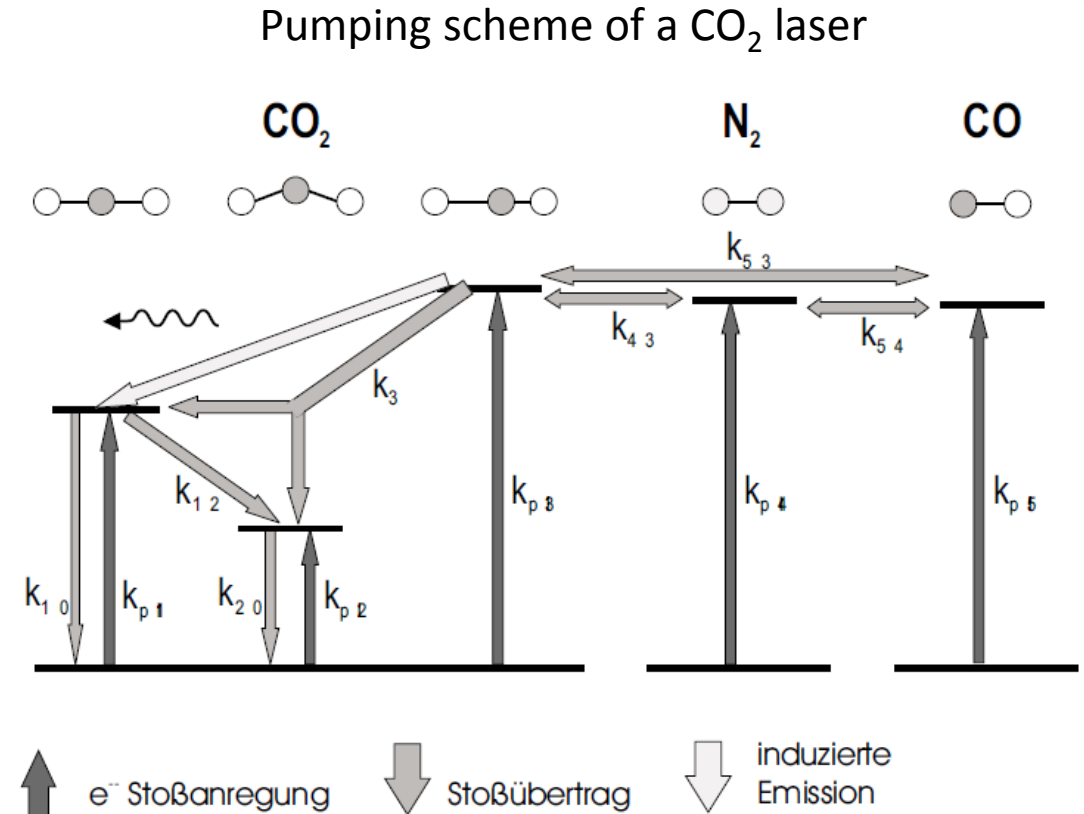
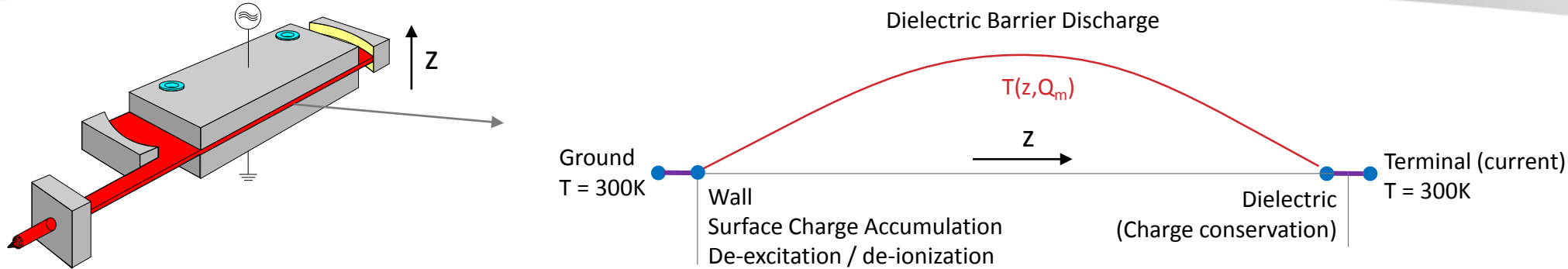


Image source: J. Schulz, Diffusionsgekühlte, koaxiale CO₂-Laser mit hoher Strahlqualität, Dissertation, RWTH Aachen (2001)

Step 2: 1D Discharge - Setup



- For stability analysis, plasma temperature has to be self-consistent
 - ▶ Parabolic temperature profile $T(z, Q_m)$
 - ▶ only dependent on *average* heat source Q_m
 - ▶ no need for solving the heat equation

- Self-consistent calculation via Global ODE*:

$$\frac{\partial Q_m}{\partial t} = (Q_{int} - Q_m) / \tau_p$$

Q_m = average heat source
 Q_{int} = integrated capacitive losses
 τ_p = averaging time constant (3...5 RF cycles)

- „Temporal“ evolution does not reflect actual thermal time scale!
- Artificial time scale τ_p ensures fast convergence to quasi-steady state

* Calculation of Q_{int} and global ODE is decoupled from plasma physics using the nojac operator and a segregated solver for better convergence

Step 2: 1D Discharge - Results

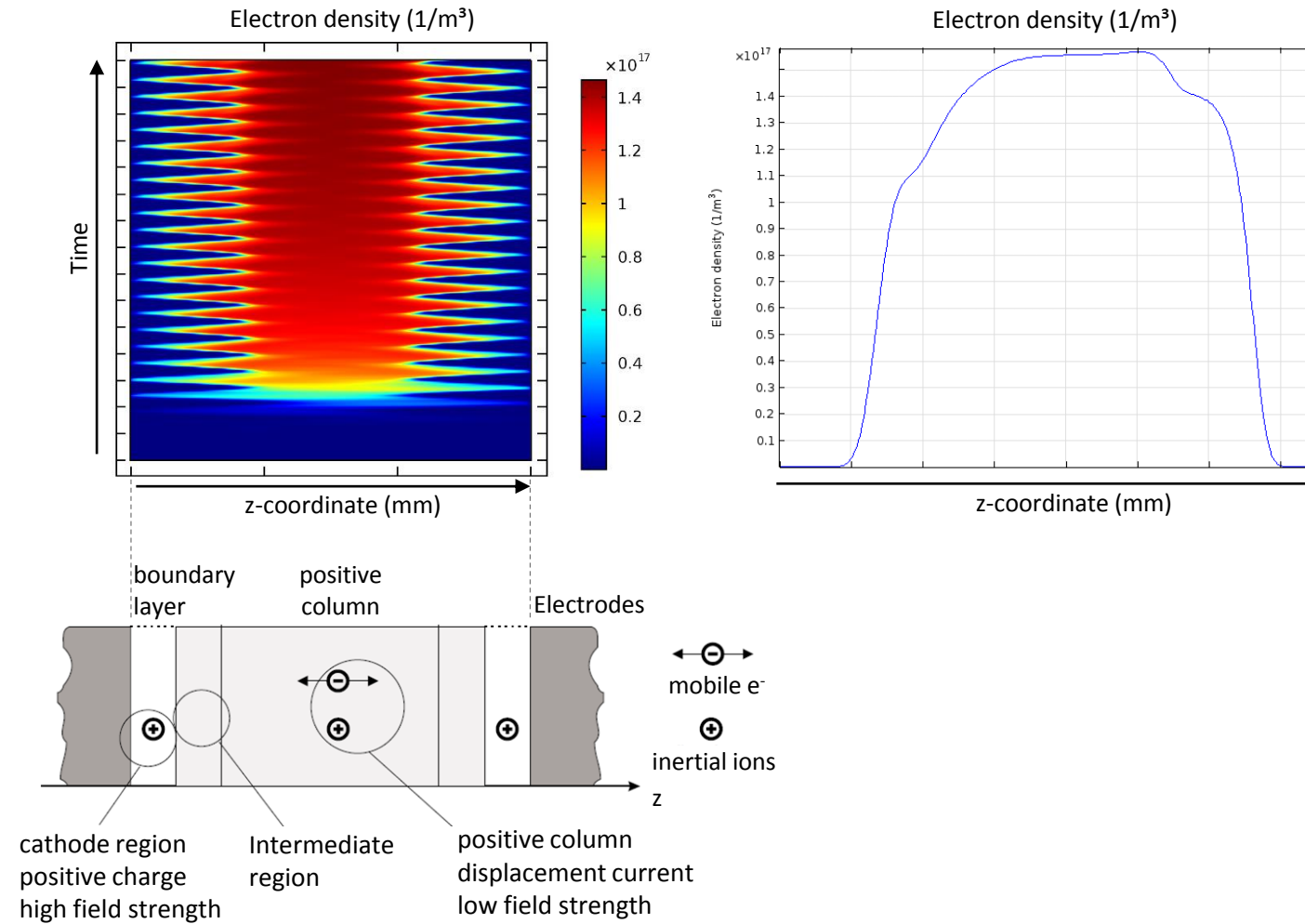
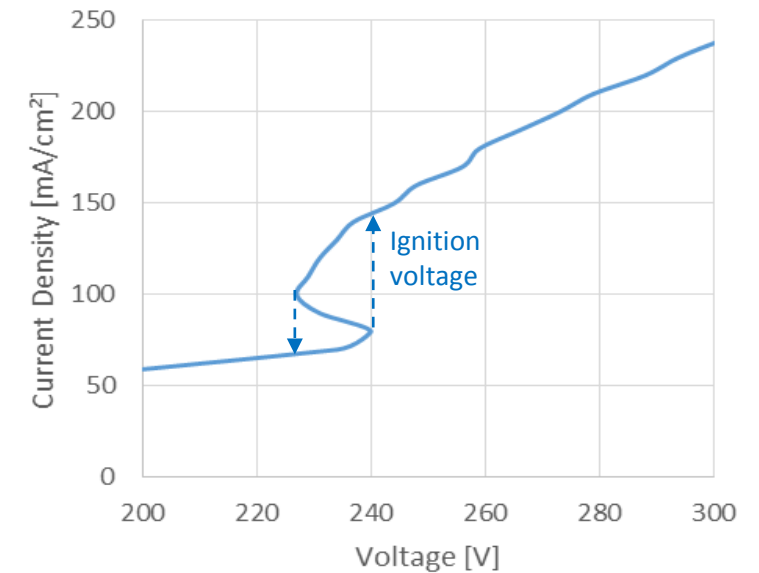


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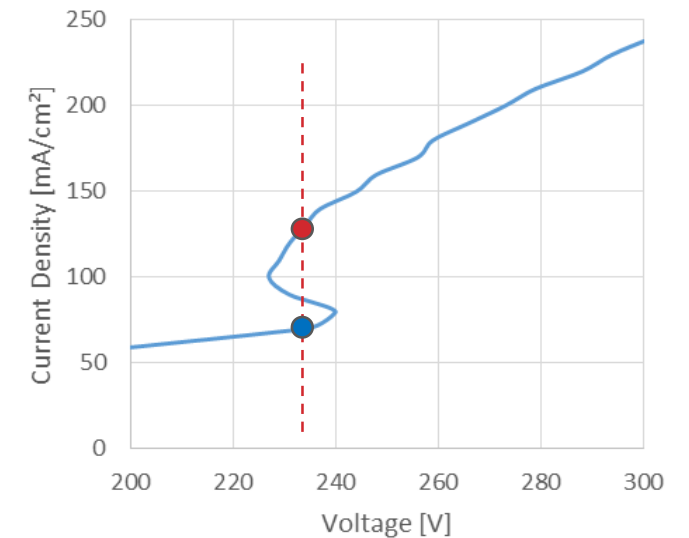
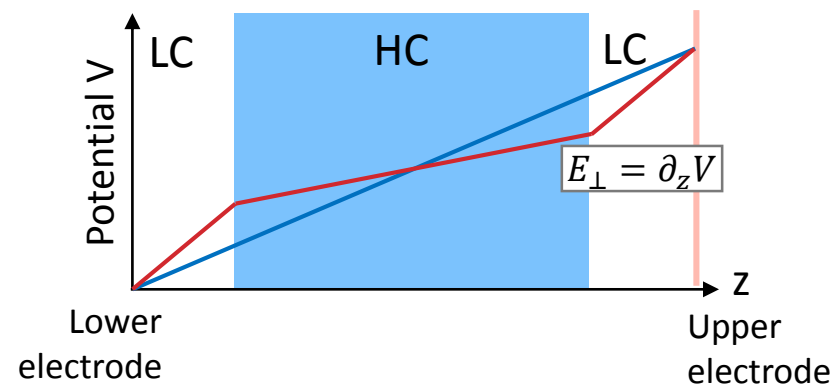
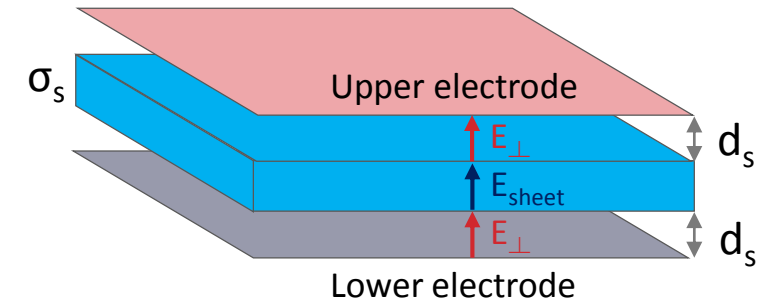
Result parameters for 3D:

- ▶ Impedance
- ▶ Temperature (cooling)
- ▶ Collision rates (laser pumping)
- ▶ Boundary layer thickness
- ▶ ...



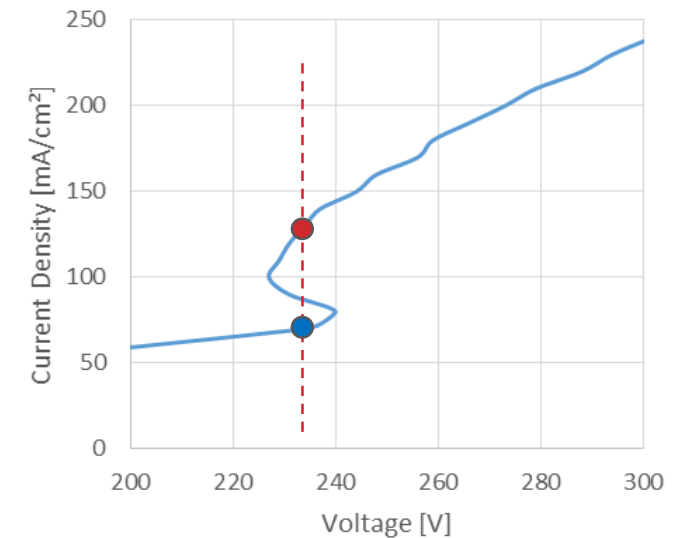
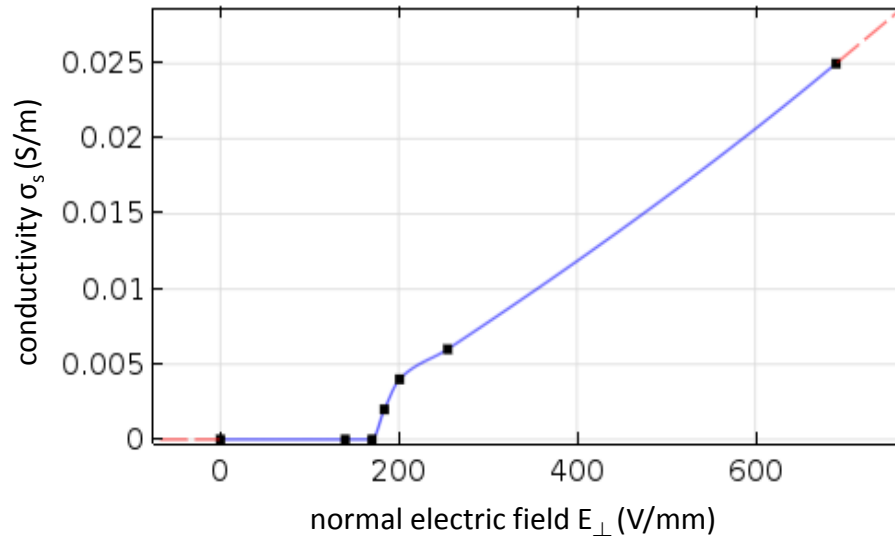
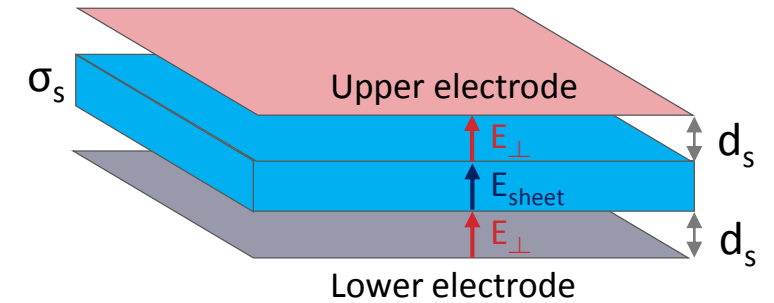
Step 3: 3D simulation – Material impedance

- Task: find a „solid“ surrogate material which resembles the same UI-curve
- Replacement of plasma discharge (steady-state properties) by „plate capacitor“ with conductive sheet (as part of a complex 3D structure)
- Evaluate normal electric field at boundary instead of terminal voltage:
 - ▶ ambiguous solutions exist for identical voltage drop
 - ▶ unique solution regarding normal field at boundary
 - ▶ Accessibility of variable



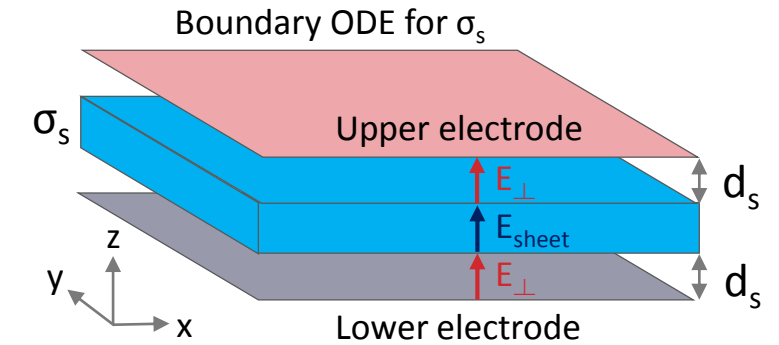
Step 3: 3D simulation – Material impedance

- Task: find a „solid“ surrogate material which resembles the same UI-curve
- Replacement of plasma discharge (steady-state properties) by „plate capacitor“ with conductive sheet (as part of a complex 3D structure)
- Interpolation function: unique, continuous, smooth

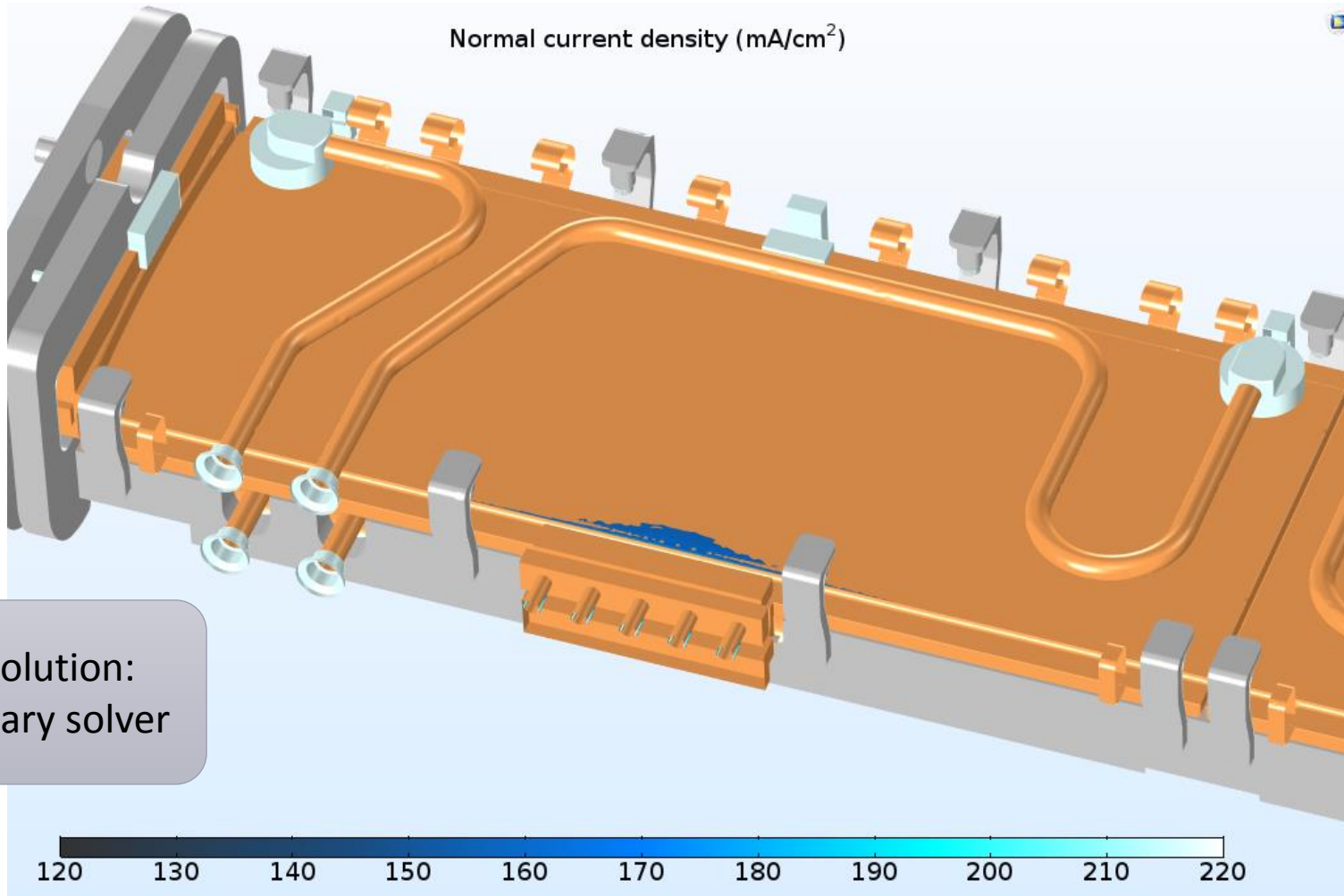


Step 3: 3D simulation – COMSOL implementation

- 3D RF simulations (emw – frequency domain)
- Upper electrode surface: „reference boundary“
 - ▶ interpolation function $\sigma_s(|E_{\perp}|)$
 - ▶ Boundary ODE: $\sigma_s - \sigma_m = 0$ (to avoid stiff matrix)
 - ▶ Model coupling (projection) from boundary to sheet volume
- Geometric multigrid solver (segregated RF / boundary ODE)
 - ▶ Number of DoFs: 6.737.446
 - ▶ Solution Time: 2 hours (8 Core CPU, 256GB RAM)

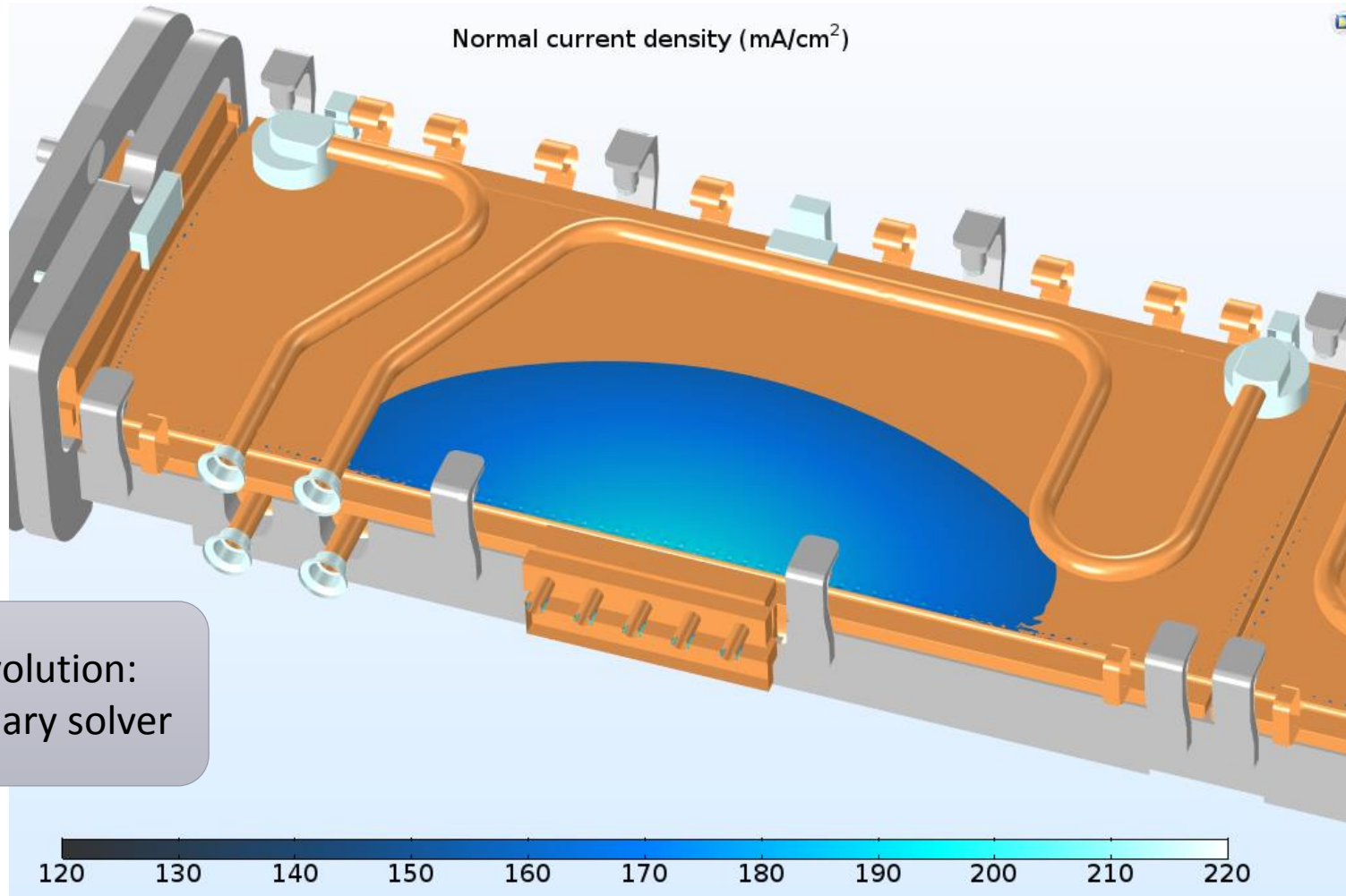


Step 3: 3D simulation – Results



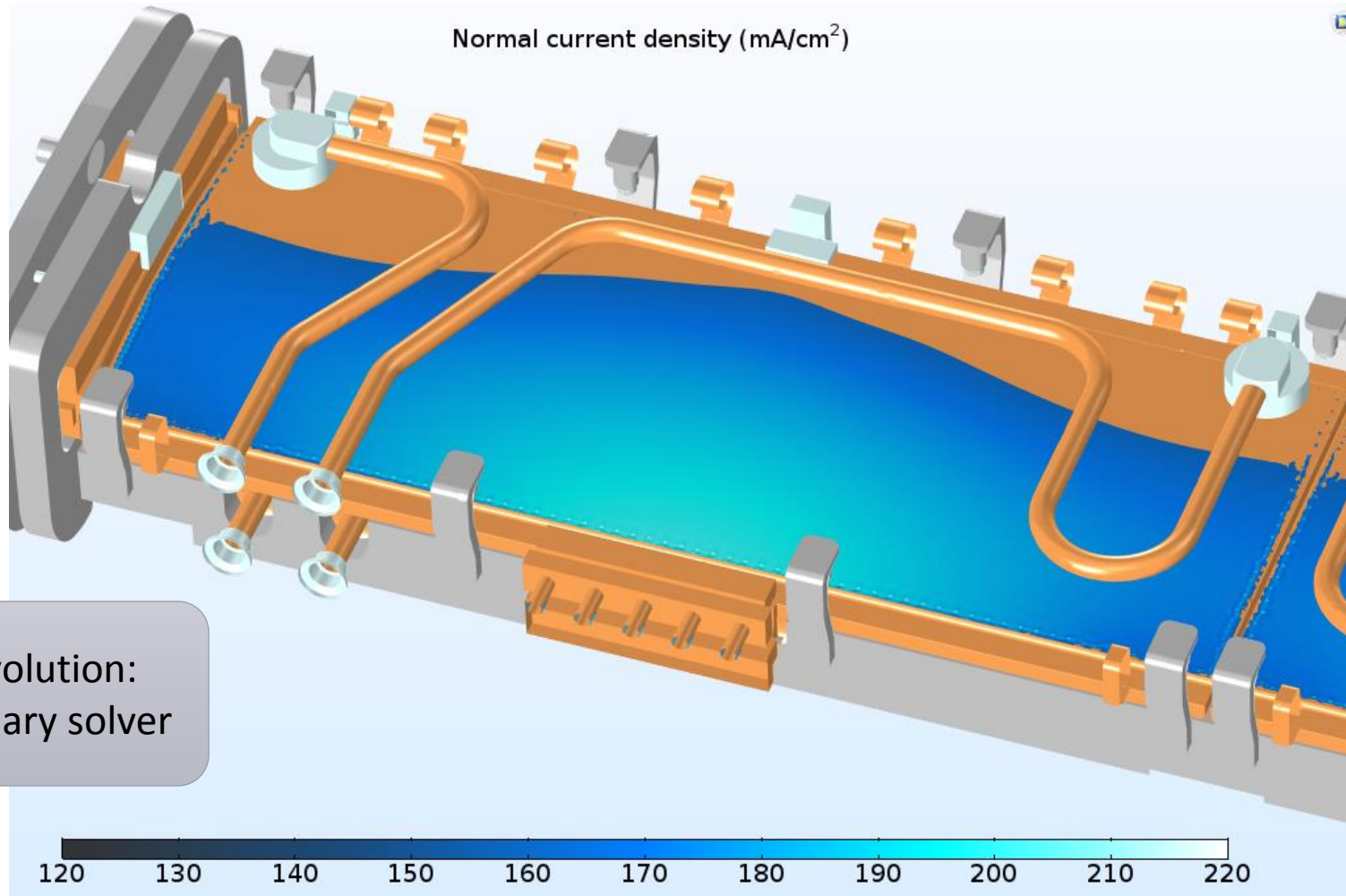
No actual time evolution:
Iterations of stationary solver

Step 3: 3D simulation – Results



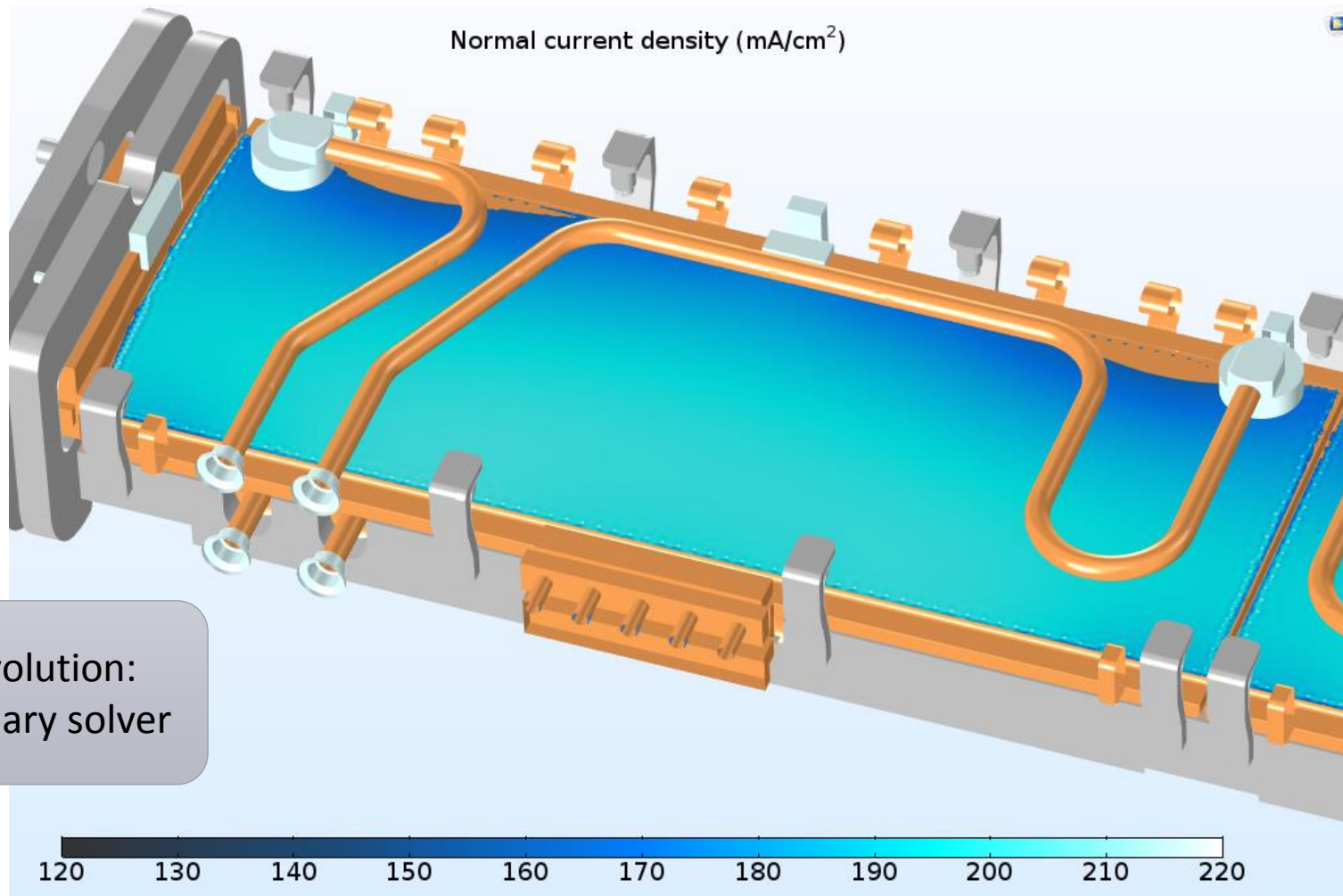
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Step 3: 3D simulation – Results



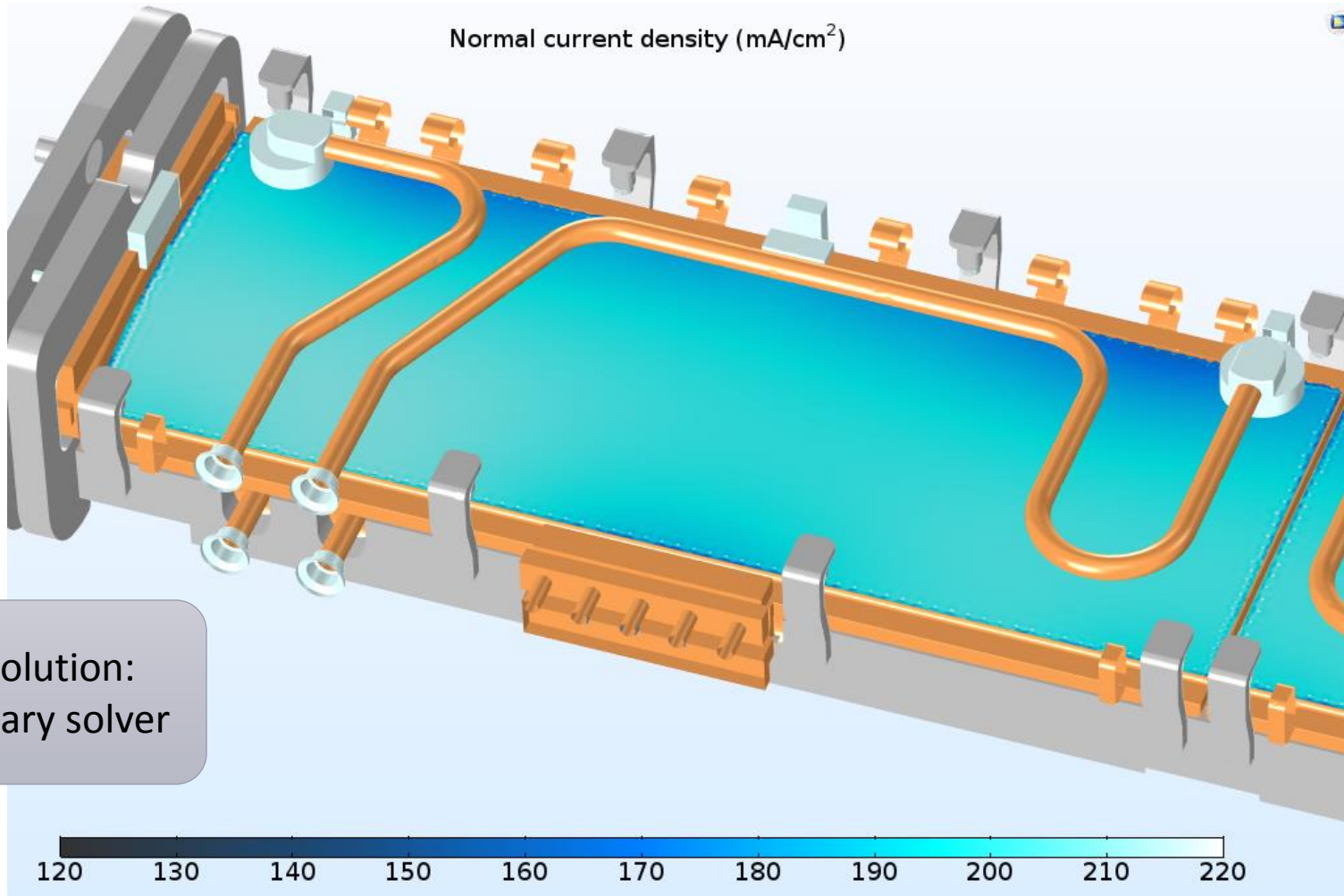
No actual time evolution:
Iterations of stationary solver

Step 3: 3D simulation – Results



No actual time evolution:
Iterations of stationary solver

Step 3: 3D simulation – Results



No actual time evolution:
Iterations of stationary solver

- Multilevel approach enables 3D simulation of a planar gas discharge in a laser
- Mutual coupling of RF field and plasma physics is maintained
- Characteristics of the discharge can be evaluated at any point in a complex 3D geometry
- Model has been successfully applied
 - ▶ Design of RF feeding / matching architecture
 - ▶ Prediction of working point for alternative gas compositions
 - ▶ Good agreement with experimental results
- Perspectives:
 - ▶ Temporal evolution of the ignition phase
 - ▶ Pressure variations during switch-on or pulsed operation
 - ▶ Further development and optimization of current and future products



Thank you for your attention.



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