

# COMSOL CONFERENCE

2014 BOSTON



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Zewail City of Science and Technology

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# Simulation of a New PZT Energy Harvester with a Lower Resonance Frequency Using COMSOL Multiphysics®

Zewail City Staff

Sep, 2014

# Outline

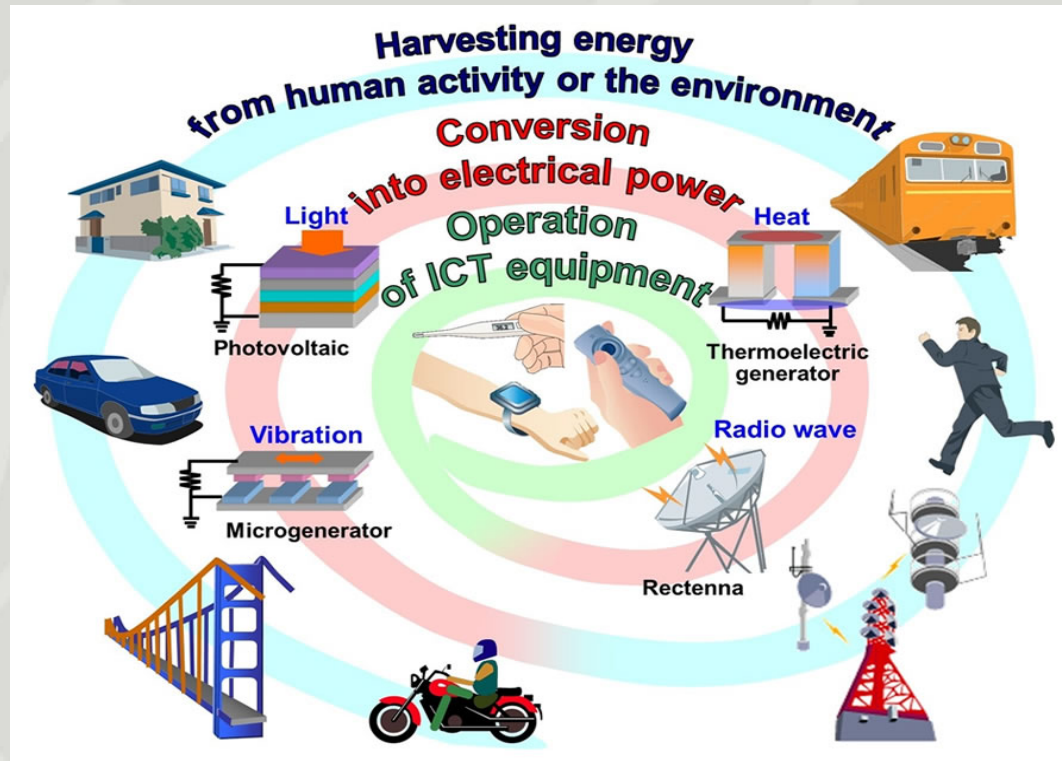
- Introduction.
- Theoretical Background of Piezoelectric Transducer.
- Use of COMSOL Multiphysics.
- Simulation Results.

# Outline

- **Introduction.**
- Theoretical Background of Piezoelectric Transducer.
- Use of COMSOL Multiphysics.
- Simulation Results.

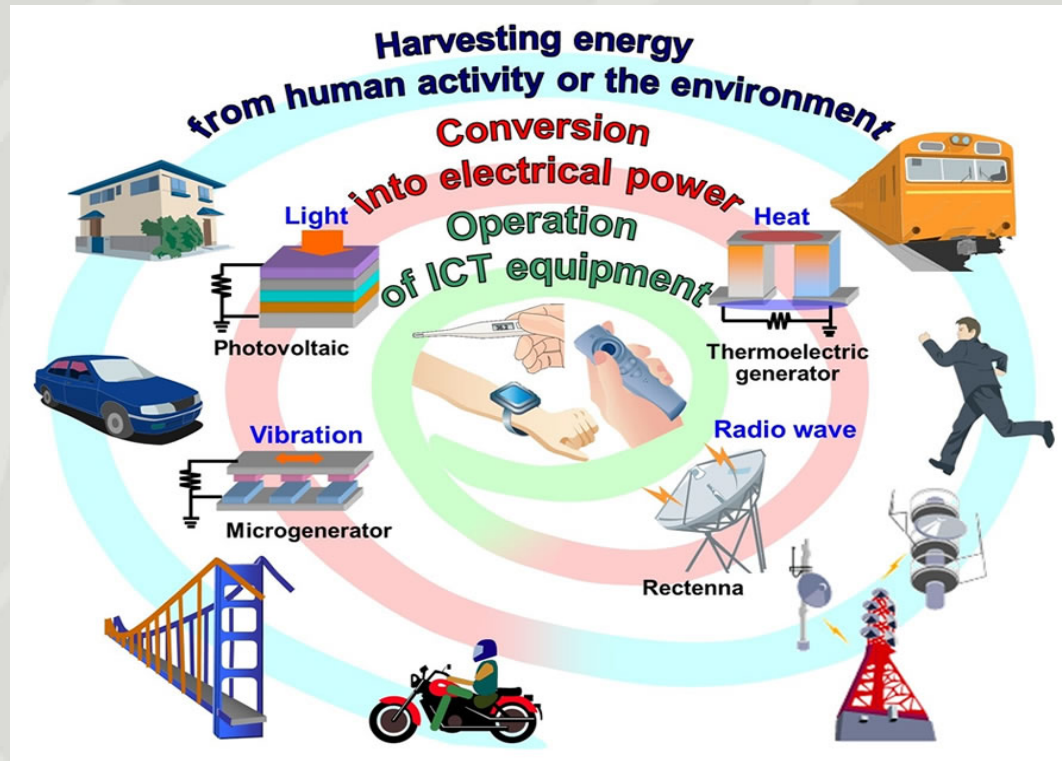
# Introduction

- Energy harvesters became a good alternative for conventional batteries.



# Introduction

- The most common sources of energy are solar radiation, vibration, and RF emissions.



# Introduction

- The most important type is the environmental vibration because of natural oscillations like that caused by air or liquid flow and by exhalation or the heartbeat of a human body.





# Introduction

- This vibration can be converted into electrical energy by three main harvesting mechanisms:
  - Electrostatic.
  - Electromagnetic.
  - Piezoelectric.

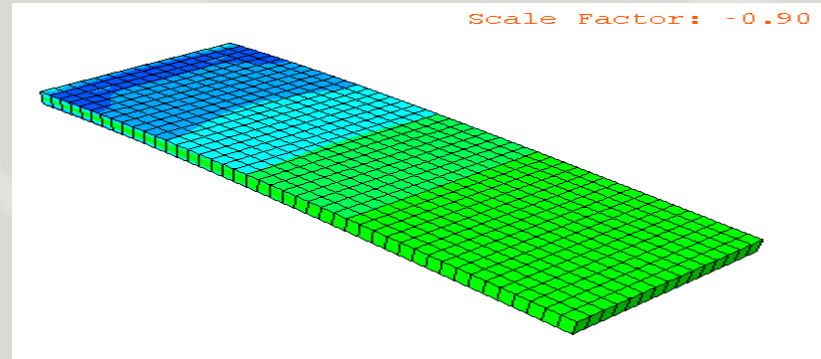


# Introduction

- **Piezoelectric Energy Harvesters**

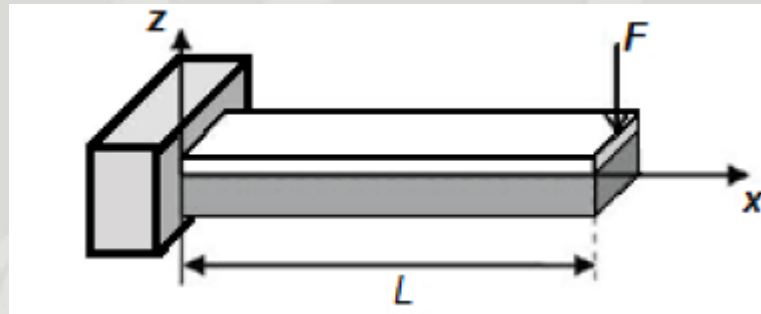
The piezoelectric materials produce electric charges when strained.

They are mostly used because they have a large power and are simple to use in applications.



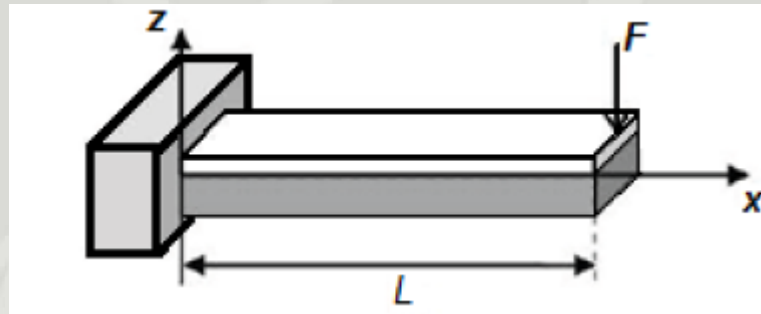
# Introduction

- The most common structure used in PEH is the cantilever beam.



# Introduction

- It is a beam with a support at one end, and is often referred to as a “fixed-free” beam.



# Outline

- Introduction.
- **Theoretical Background of Piezoelectric Transducer.**
- Use of COMSOL Multiphysics.
- Simulation Results.

# Theoretical Background of Piezoelectric Transducer

- The form used to describe the behavior of piezoelectric material is strain-charge form.

$$S = s^E T + d \bar{E}$$
$$D = d T + \epsilon^T \bar{E}$$

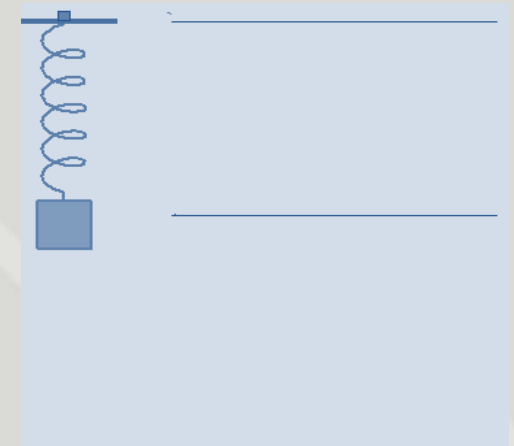
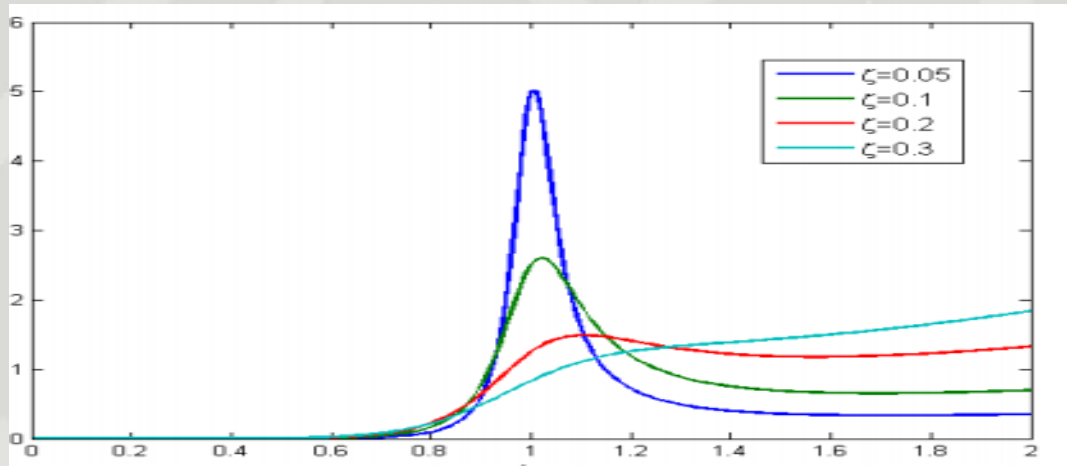
- The second term in the right side of first equation represents the piezoelectric coupling term, which provides the mechanism for energy conversion.

# Theoretical Background of Piezoelectric Transducer

- One of the most important design parameters in designing a vibration energy harvesting device is the resonant frequency.

# Theoretical Background of Piezoelectric Transducer

- Maximum energy occurs when the vibration frequency of the environment matches the resonant frequency of the cantilever .





# Theoretical Background of Piezoelectric Transducer

- The variation of resonant frequency as follows

$$f_n \propto \frac{1}{L^2} \sqrt{t_p} \sqrt{t_s}$$

where

$L$ : length of cantilever.

$t_p$  : thickness of piezoelectric material.

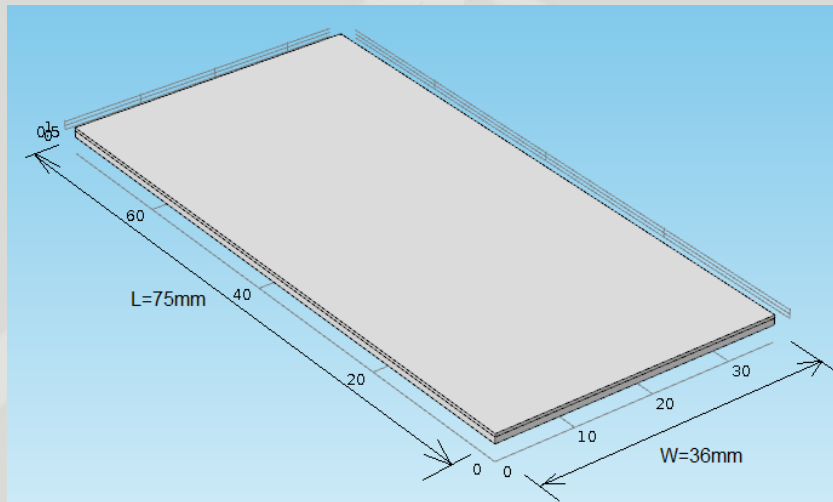
$t_s$  : thickness of substrate material

# Outline

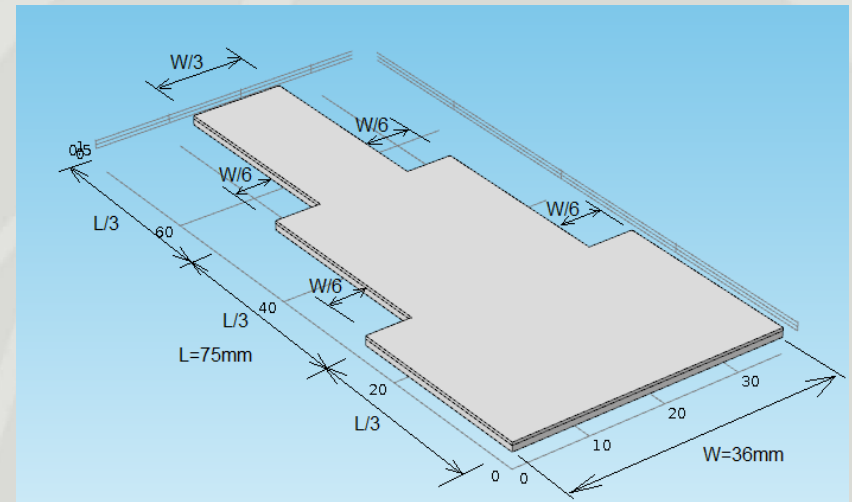
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# Use of COMSOL Multiphysics

- The proposed and rectangular shapes were designed and simulated.



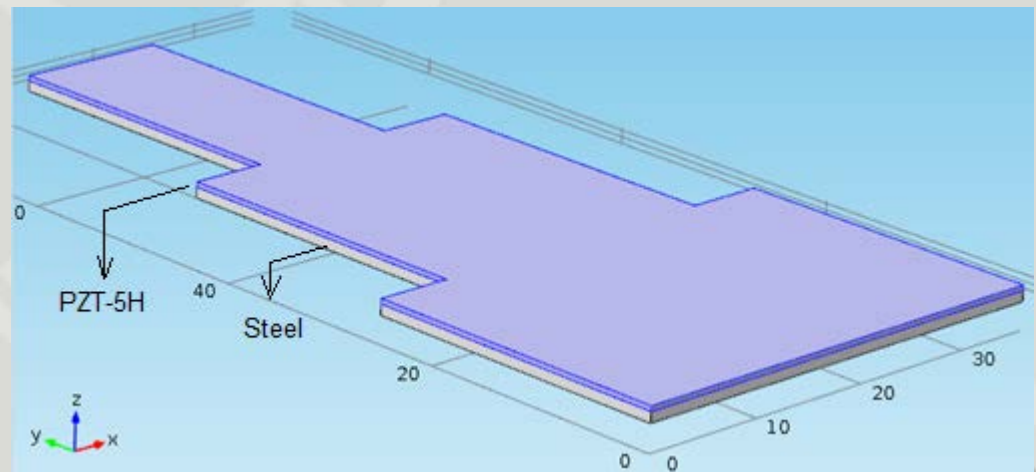
**Rectangle Geometry**



**Proposed Geometry**

# Use of COMSOL Multiphysics

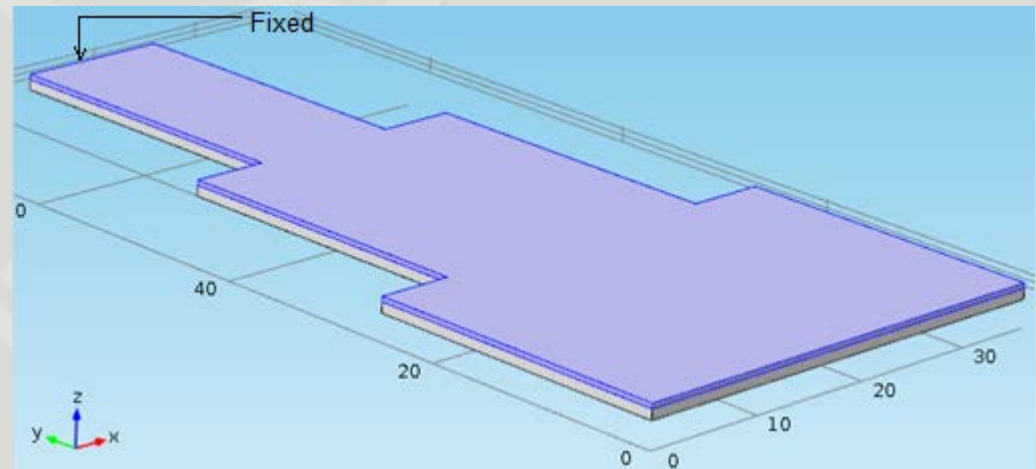
- The lower and upper layers are chosen to be steel and Lead Zirconate Titanate (PZT-5H).



# Use of COMSOL Multiphysics

- **Boundary Conditions**

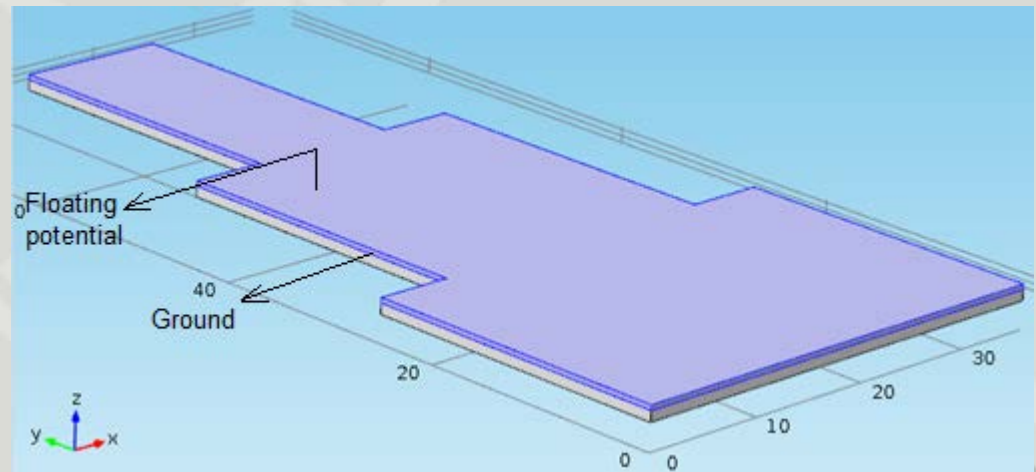
- The narrow end of the unimorph cantilever is fixed while other is free to vibrate.



# Use of COMSOL Multiphysics

- **Boundary Conditions**

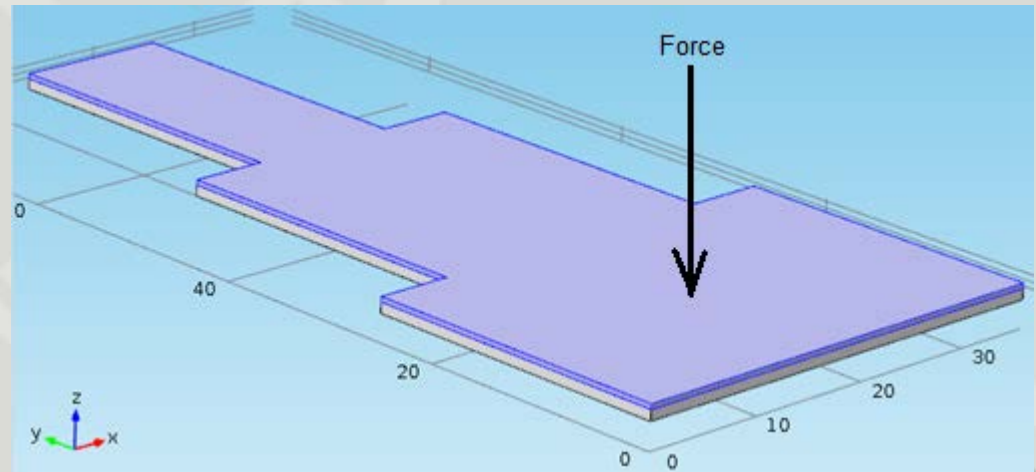
- The floating potential and grounding are applied at the upper and the lower face of the piezoelectric layer respectively.



# Use of COMSOL Multiphysics

- **Boundary Conditions**

- The body load  $F$  (0.1N) is applied as an input to the piezoelectric layer to induce a strain.

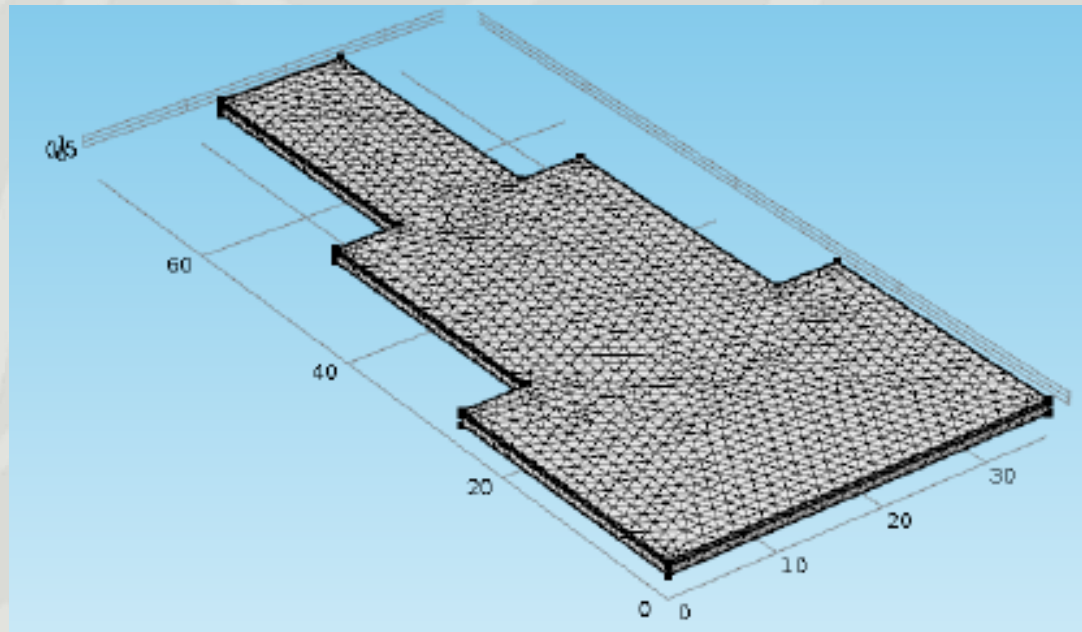




# Use of COMSOL Multiphysics

- **Meshing**

- The model is meshed in tetrahedral blocks with fine element size.



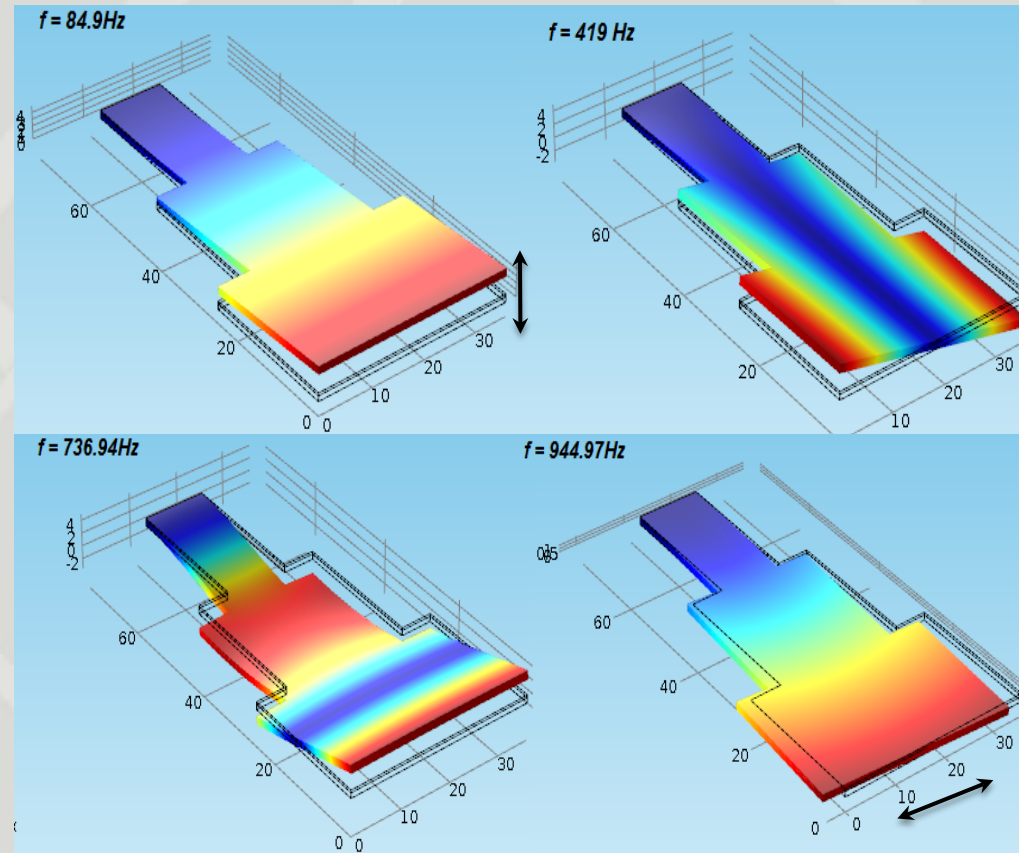
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- **Simulation Results.**

# Simulation Results

- **Eigenfrequency Analysis**

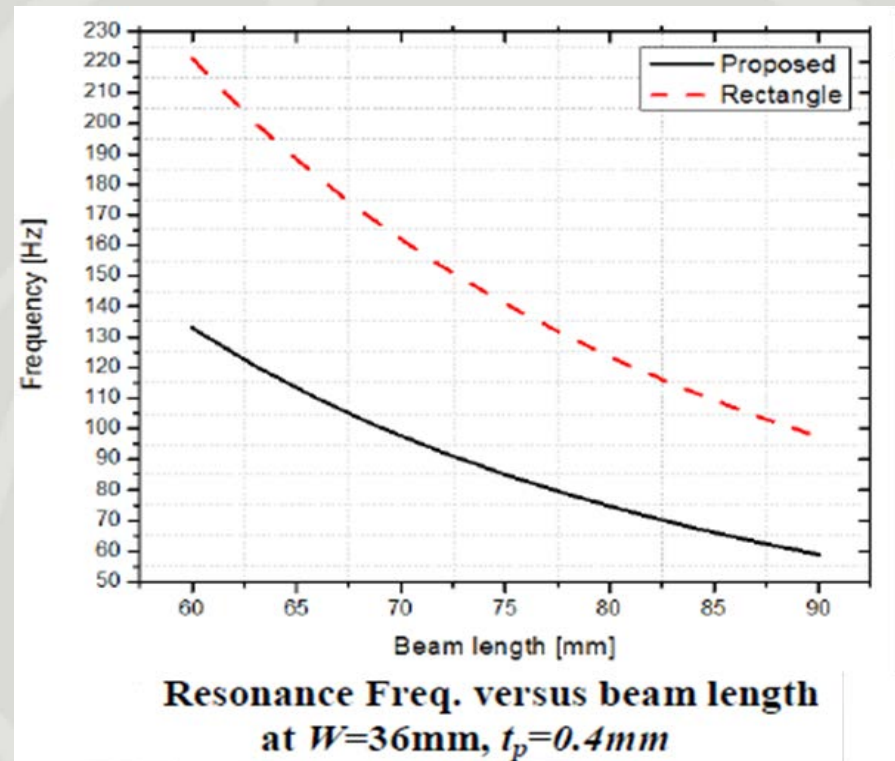
The first four resonance frequencies of proposed geometry.



# Simulation Results

- **Eigenfrequency Analysis**

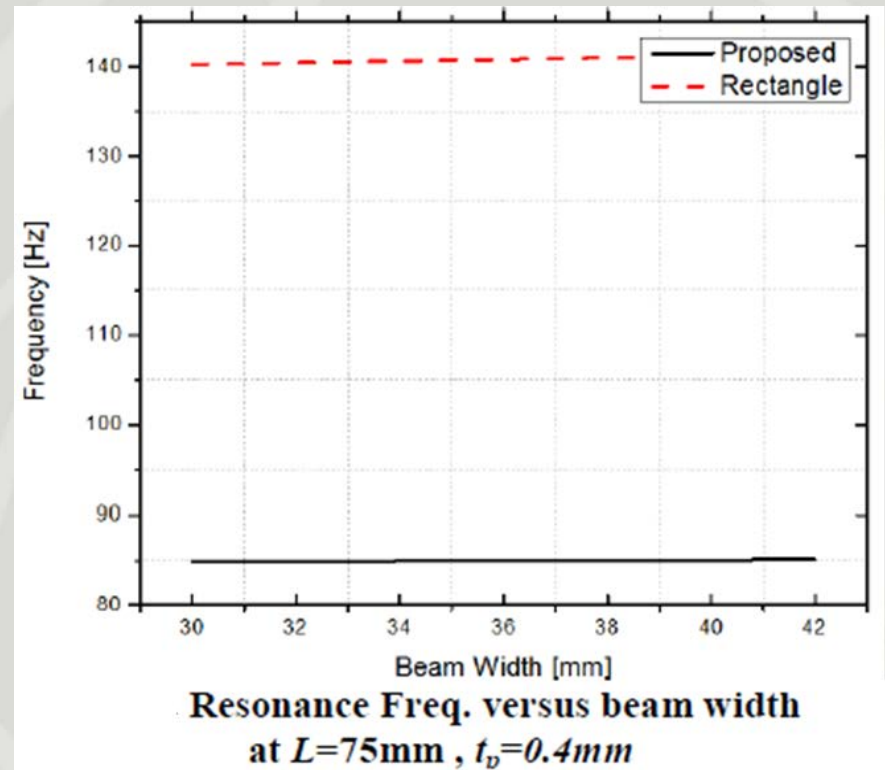
The resonant frequency decreases with increasing the cantilever length.



# Simulation Results

- **Eigen frequency Analysis**

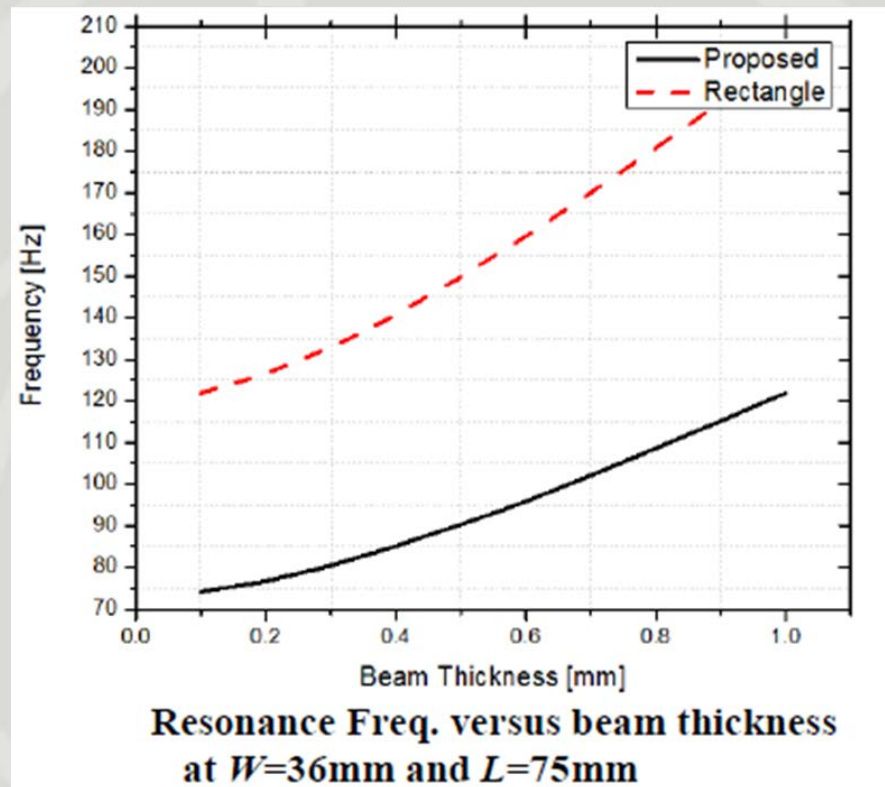
The resonant frequency is slightly invariant to the width of cantilever.



# Simulation Results

- **Eigen frequency Analysis**

The resonant frequency increases with increasing the cantilever thickness.



# Simulation Results

- **Eigen frequency Analysis**

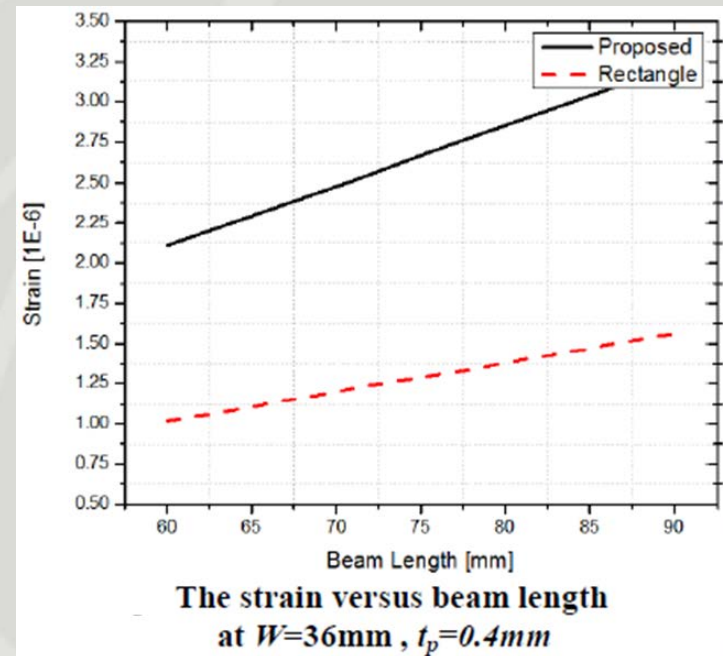
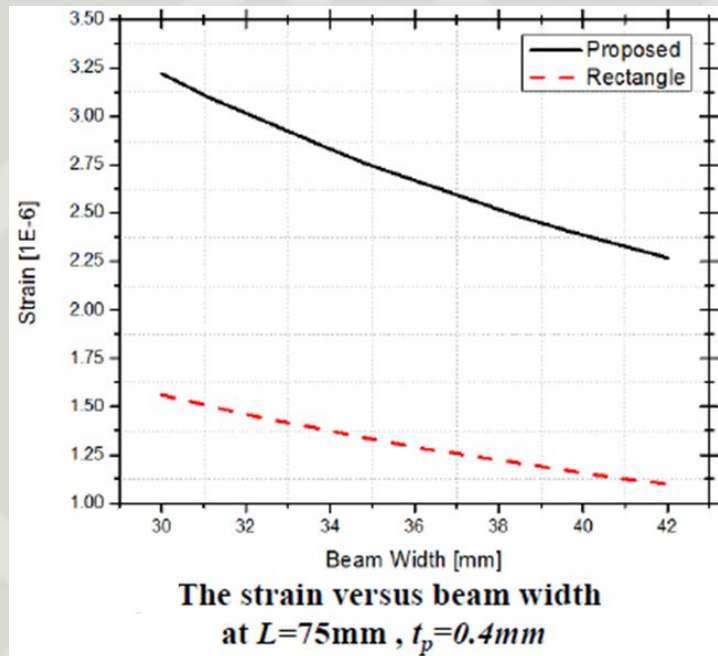
It is clear that with the same width, length, and thickness the proposed geometry has a lower resonant frequency than generated from the rectangle one which make this proposed geometry is more suitable for human applications.



# Simulation Results

- **Stationary Analysis**

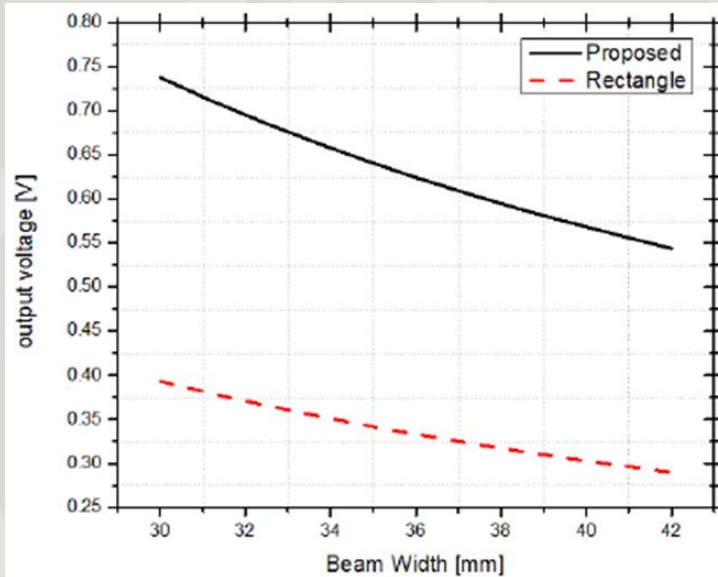
the proposed geometry has a larger strain than obtained from the rectangle shape.



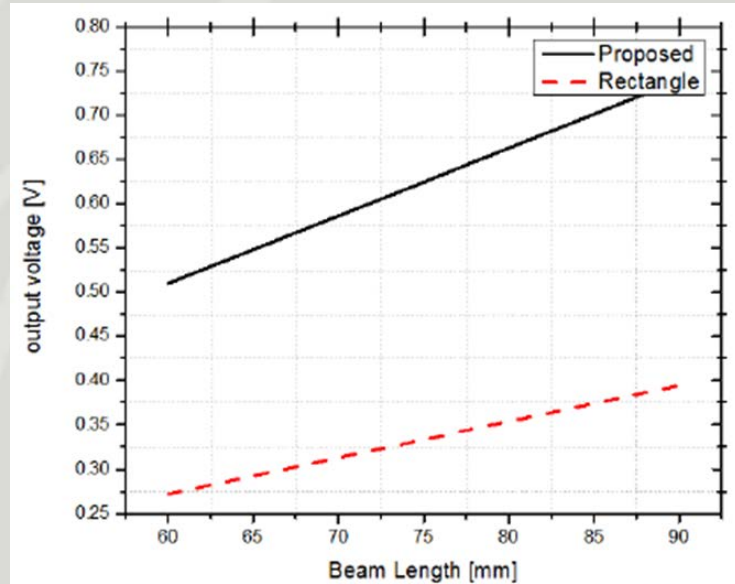
# Simulation Results

- **Stationary Analysis**

the proposed geometry has a larger output voltage than obtained from the rectangle shape.



The output voltage versus beam width  
at  $L=75\text{mm}$  ,  $t_p=0.4\text{mm}$



The output voltage versus beam length  
at  $W=36\text{mm}$  ,  $t_p=0.4\text{mm}$

# Simulation Results

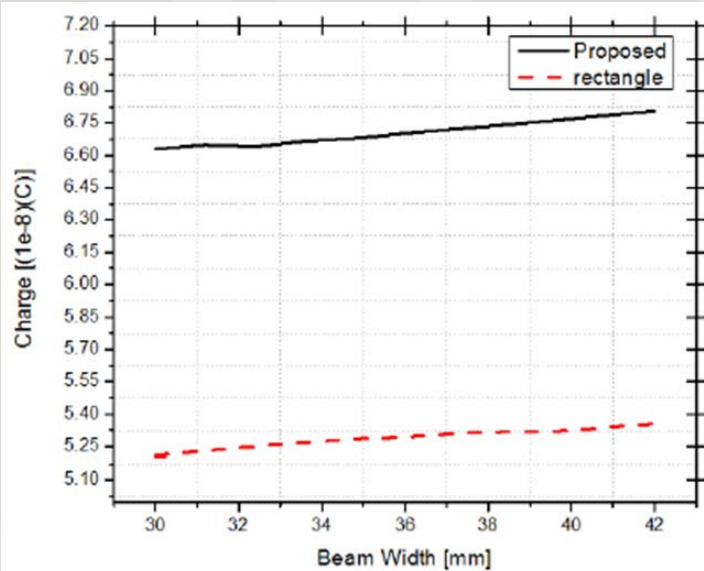
- **Stationary Analysis**

After integrating the surface charge density over the piezoelectric surface, the total stored charge was calculated.

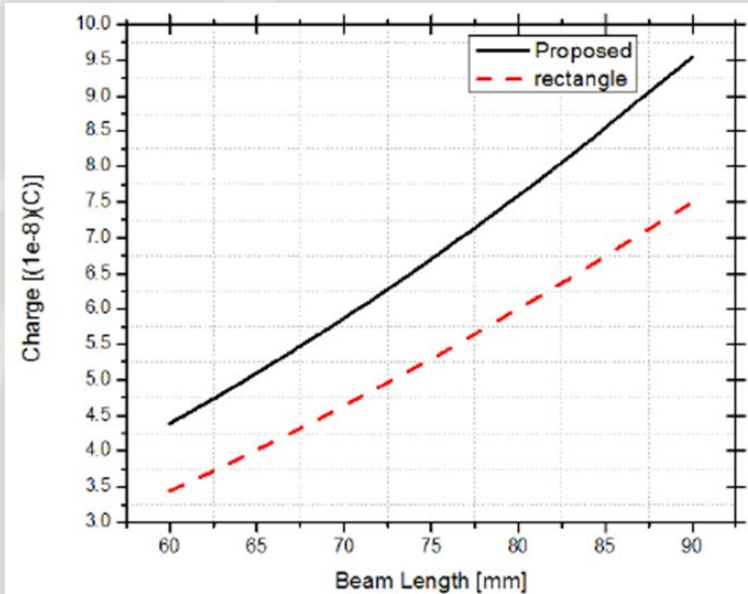
# Simulation Results

- Stationary Analysis**

Increasing the beam length and width increases the total charge.



The generated charge versus beam width at  $L=75\text{mm}$ ,  $t_p=0.4\text{mm}$

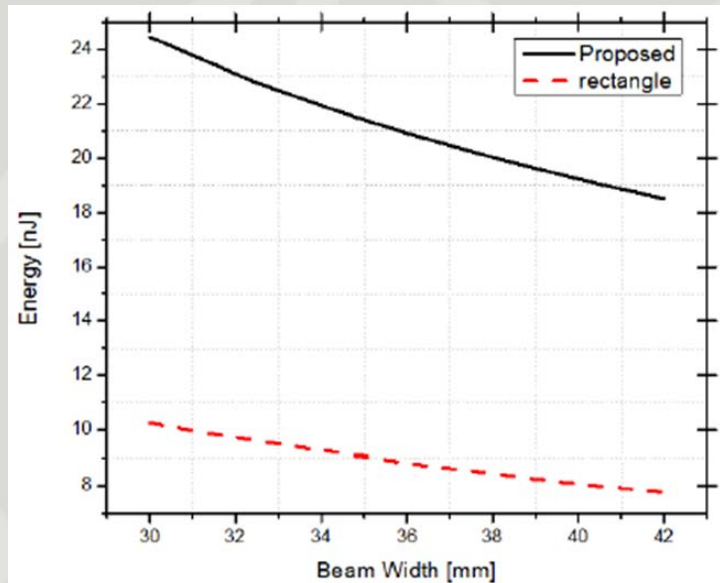


The generated charge versus beam length at  $W=36\text{mm}$ ,  $t_p=0.4\text{mm}$

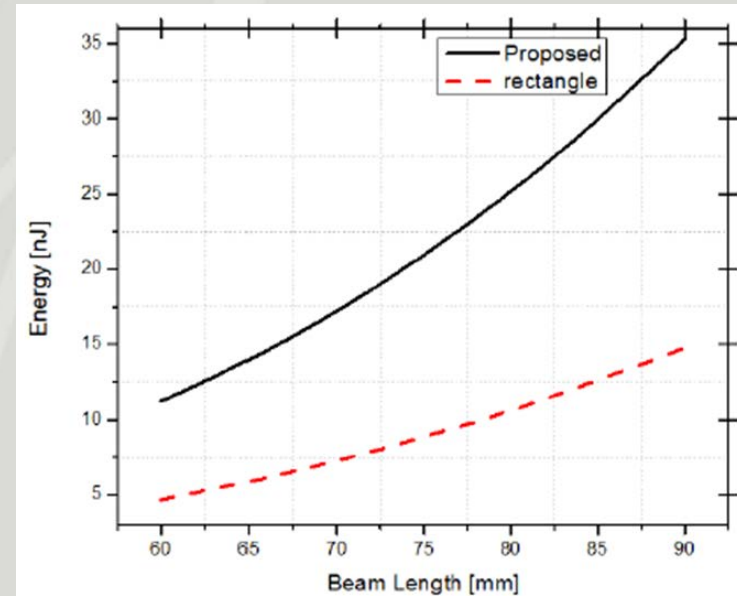
# Simulation Results

- **Stationary Analysis**

The total stored energy was calculated using this equation

$$E = \frac{1}{2} QV$$


Energy versus beam width  
at  $L=75\text{mm}$ ,  $t_p=0.4\text{mm}$



Energy versus beam length  
at  $W=36\text{mm}$ ,  $t_p=0.4\text{mm}$

# Thank You