

# An Equivalent Kd-based Radionuclide Transport Model Implemented in COMSOL Multiphysics® Software

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## Abstract

The Swedish Nuclear Fuel and Waste Management Company (SKB) has developed conceptual and quantitative models for the reactive transport of selected radionuclides in the near-surface system or regolith (Grandía et al., 2007; Sena et al., 2008; Piqué et al., 2010). However, the description of hydrological processes and the model geometries were simplified, due to computational constraints and the limitations of the available reactive transport tools

Radionuclide sorption is often simulated using a lumped approach where retention processes are represented by a single parameter, the distribution coefficient (Kd), which relates the radionuclide mass retained in the solid phase to its aqueous concentration. Kd-based simulations rely on two strong assumptions: Kd depends on soil properties and is constant in time. However, sorption processes depend also on the fluid characteristics, which can be spatially and temporally variable.

Here, a 3D mechanistic reactive transport model of the regolith was implemented in iCP (Nardi et al., 2014). The result of this model provides a dataset of Kd values representative of the actual geochemical conditions of the regolith. That dataset is used to build equivalent 3D Kd-based models describing the retention of <sup>90</sup>Sr, <sup>137</sup>Cs, <sup>235</sup>U and Ra. The model was implemented in Comsol using the Darcy's Law (Subsurface Flow module, Fluid Flow), and Solute Transport (Chemical Species Transport module) physics and accounts for steady state saturated-unsaturated flow assuming constant recharge and radionuclide transport with linear sorption. Also, high resolution of 3D hydrological and geological conditions in the regolith is considered.

Two types of Kd interpretation were compared: "equivalent Kd spatial field" versus "2-single time dependent Kd values". The first approach determines Kd values using the concentration distributions of dissolved (Figure 2a) and retained (Figure 2b and c) radionuclides at the end of the iCP simulation. This generates a unique spatial field for each radionuclide (Figure 2d). The second approximation determines a spatially averaged Kd value for each layer that varies with time. This generates a temporal Kd function for the till material and another one for the clay (Figure 2e).

Overall, breakthrough curves show discrepancies between both equivalent  $K_d$ -based transport models and the fully reactive transport model (Ra and Sr present some better fit). The  $^{137}\text{Cs}$  evolution suggests that the 2-single time dependent  $K_d$  values approach is better than the equivalent  $K_d$  spatial field approach (Figure 3a and 3b). Spatial distributions of retained radionuclides and their temporal evolution show that the formulation based on 2-single time dependent  $K_d$  values reproduces the retention behavior of  $^{90}\text{Sr}$  and  $^{137}\text{Cs}$  (Figure 3c) better than the equivalent  $K_d$  spatial field approach, while this reproduces the retention behavior of  $^{235}\text{U}$  and Ra (Figure 4) better than the former. This is because the dominant retention processes of  $^{90}\text{Sr}$  and  $^{137}\text{Cs}$  are mainly dynamic, while the main mechanisms of  $^{235}\text{U}$  and Ra retention undergo local spatial variations that dominate over the temporal changes.

The equivalent  $K_d$ -based transport model could be improved by approaches accounting for a dynamic update of the  $K_d$  values or by other alternative non-local in time and space approximations.

## Reference

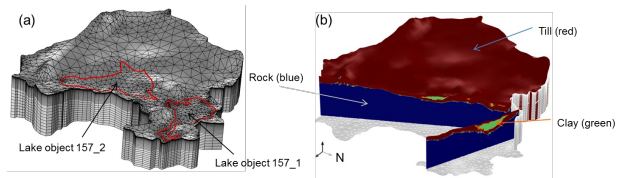
Grandía, F., Sena, C., Arcos, D., Molinero, J., Duro, L., Bruno, J., 2007. Quantitative assessment of radionuclide retention in the near-surface system at Forsmark. Development of a reactive transport model using Forsmark 1.2 data. SKB R-07-64, Svensk Kärnbränslehantering AB.

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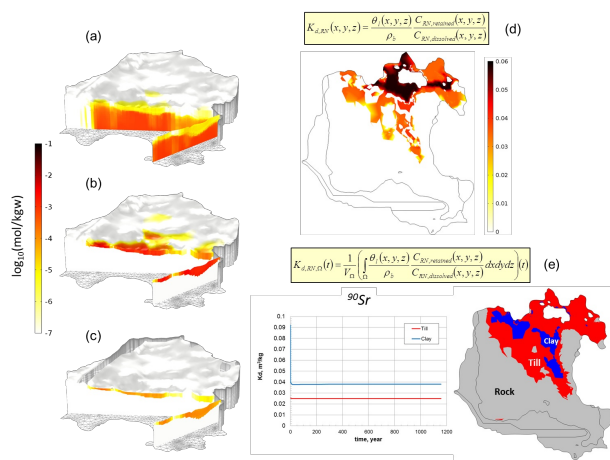
Piqué, À., Grandía, F., Sena, C., Arcos, D., Molinero, J., Duro, L., Bruno, J., 2010. Conceptual and numerical modelling of radionuclide transport in near-surface systems at Forsmark. SR-Site Biosphere. SKB-R-10-30, Svensk Kärnbränslehantering AB.

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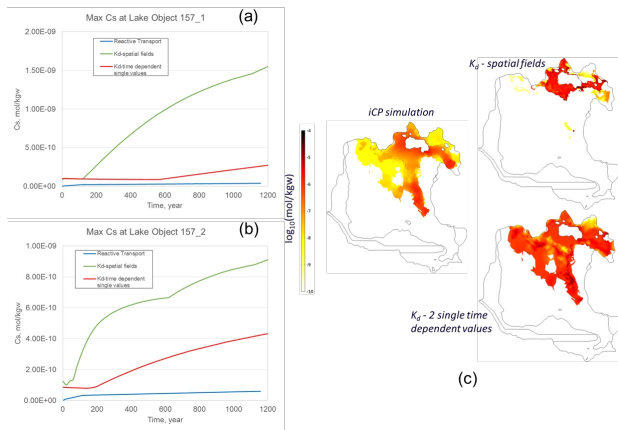
## Figures used in the abstract



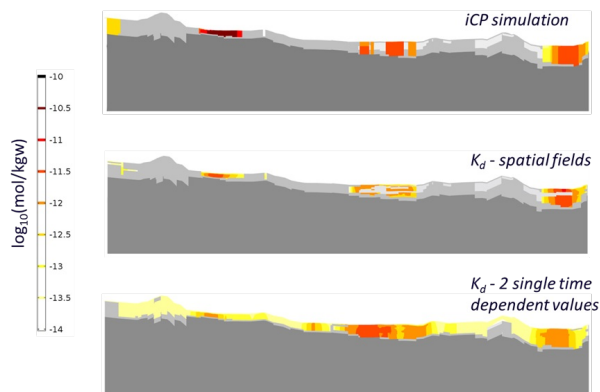
**Figure 1:** (a) 3D mesh indicating the location of the two discharge objects and the vertical discretization in the two blocks (vertical exaggeration  $\times 10z$ ). (b) Geochemical model subdomains. The granitic rock (blue) is considered inert and the regolith is divided into till and clay domains.



**Figure 2:**  $K_d$  interpretation methodology (retention of  $^{90}\text{Sr}$ ): 3D Distributions of (a) dissolved  $^{90}\text{Sr}$ , (b)  $^{90}\text{Sr}$  adsorbed on planar sites and (c)  $^{90}\text{Sr}$  precipitated as strontianite are used to calculate the (d) equivalent  $K_d$  spatial field and the (e) 2-single time dependent  $K_d$  values.



**Figure 3:** Evolution of the maximum concentration of  $^{137}\text{Cs}$  at the 157\_1 (a) and 157\_2 (b) lake objects. (c) Concentration of retained  $^{137}\text{Cs}$  simulated with iCP (fully reactive transport model) compared with the concentrations of retained  $^{137}\text{Cs}$  simulated with the equivalent  $K_d$ -based transport models ( $z = 3$  m, after 1100 years of simulation).



**Figure 4:** Concentration of retained Ra simulated with iCP (fully reactive transport model) compared with the concentrations of retained Ra simulated with the equivalent  $K_d$ -based transport models (Valley cross section, after 1100 years of simulation).