## Study of Fracture Parameter Using COMSOL-multiphysics For **Curved Cracked Bimodular Flexural Specimen** Awani Bhushan<sup>1</sup>, S. K. Panda<sup>1</sup>, 1. Indian Institute of Technology (BHU), Varanasi-221005, Uttar Pradesh, India; .

**Introduction**: Effect of bi-modularity on complex J-integral in curve cracked three point bend specimen has been presented here.



**Results**: Analysis of Von-Mises Stress around the crack-tip



(b)



## Figure1

**Computational Methods**: Using stress dependent elasticity considering different Young's modulus of elasticity in tension and compression shown in table 1. The complex J-integral for 2D semicircular geometry has been evaluated, following equation in elastic bi-modular region derived by Khan. et. al, in 2010 [1]

(a) **Figure 3**. Von-Mises stress distribution (a) for whole geometry (b) around the Crack tip



Figure 4. Young's Modulus plot (a) Representing the region of tension and compression and (b) Normal stress variation in the vertical cut line at quarter length from the



$$\hat{J}_{F} = \int_{\Gamma_{A}} (W\hat{n}_{\beta} - \hat{T}_{i}\hat{u}_{i;\beta})d\Gamma - \int_{A} \frac{1}{r}\hat{\sigma}_{i\beta}\hat{u}_{i;r}dA + [\int_{A} \hat{\sigma}_{ij}\hat{\varepsilon}_{ij;\beta}^{th}dA + \int_{A} \hat{\sigma}_{ij}\hat{\varepsilon}_{ij;\beta}^{th}dA + \int_{A} \hat{\rho}\hat{u}_{i}\hat{u}_{i;\beta}dA - \int_{A} \hat{B}_{i}\hat{u}_{i;\beta}dA]$$

$$\int_{A} \hat{\sigma}_{ij}\hat{\varepsilon}_{ij;\beta}^{0}dA + \int_{A} \hat{\rho}\hat{u}_{i}\hat{u}_{i;\beta}dA - \int_{A} \hat{B}_{i}\hat{u}_{i;\beta}dA]$$

In elastic bi-modular stress field, the integrals due to material inertial, thermal stresses, initial strain and body forces vanishes and expression reduced to  $\hat{J}_{F} = \int_{\Gamma} (W\hat{n}_{\beta} - \hat{T}_{i}\hat{u}_{i;\beta})d\Gamma - \int_{\Lambda} \left(\frac{1}{r}\hat{\sigma}_{i\beta}\hat{u}_{i;r}\right)dA$ 



**Figure 5**.Comaparision of Normalized complex *J*-integral vs Rice's J-integral (for  $E_T/E_C$  ratio =1.83) at all contours

**Conclusions**: The degree of path independency for complex J-integral  $\hat{J}_{F}$  in the comparison of Rice's Jintegral [2] is found to very good. The  $E_T/E_C$  ratio influences the value of the complex J-integral significantly as observed by the simulation of nuclear grade graphite grade (2020). Therefore, it is concluded that the effect of the bi-modularity on the computation of complex *J*-integral  $\hat{J}_{F}$  values cannot be neglected.

## Figure 2. Comsol modular mesh around the crack tip for

**References**:

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