Numerical Modeling of Wave Propagation in Particulate Composites

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Abstract: Syntactic foam composites are used as core materials in sandwich structures due to their attractive mechanical and physical properties such as high compressive strength, low moisture absorption, etc. Nondestructive characterization of these materials using techniques such as Ultrasound is performed extensively in order to study the effect of processing conditions on the porosity observed. Fundamental factor which dictates the ultrasonic behavior of these particulate composites is the ratio of wavelength to particle size ratio. Experimental studies to determine the interaction between ultrasonic wave and the particle existing in these composites is difficult. Hence, a 2-D transient pressure acoustics finite element model using COMSOL 4.2 is considered to understand the effect of wave length to a particle size ratio on the wave propagation. Three different cases of ratio of wave length to particle size equal to, greater than, and lesser than one, are considered. It is observed that the wavelength plays a predominant role on the wave scattering behavior in these composites.

Keywords: Syntactic foams, Wavelength to particle size ratio, Absorption, Finite Element Method, Modeling.

1. Introduction

Syntactic foams are light-weight particulate composites made from a mixture of a polymer resin and hollow particles, called microballoons [1]. Several studies have been conducted on the use of microballoons made from different materials such as steel, aluminum and glass. However, glass microballoons have emerged as the most attractive alternative for use as fillers in particulate composites because of their high strength, low density and manufacturing ease. Glass microballoons as shown in Figure 1 have an outer and inner diameter. The difference between outer and inner diameter is termed as wall thickness ‘t’.

Syntactic foams possess attractive mechanical and physical properties such as high compressive strength [2, 3], low moisture absorption [4, 5] and low coefficient of thermal expansion, making them an attractive material for use in aerospace and marine applications. With increasing use of these materials in aerospace and marine applications, there is a need to evaluate these materials non-destructively, using non-destructive evaluation (NDE) techniques such as ultrasound. Ultrasonic imaging has emerged as the most promising of all NDE technologies because of its high sensitivity and accuracy in determining cracks, defects and physical properties in a structure, and its simplicity of use, ease of application, and cost effectiveness [6]. Pulse echo and through transmission ultrasonic techniques are mainly used for characterization of materials. Knowledge of attenuation coefficient along with longitudinal and shear wave velocities are required for characterizing syntactic foams and other porous materials using Ultrasonic Imaging (UI) technique [7].

Several theoretical studies are found in the published literature dealing with the ultrasonic characterization of random particulate composites by considering single [8-10] and multiple scattering of particles [11-16]. The major disadvantage with theoretical estimates is that they are difficult in quantifying the results. Numerous experimental studies are also found in the literature dealing with the ultrasonic characterization of periodic [17], and random particulate composites [18-23]. Most of these studies are focused on the evaluation of ultrasonic properties in solid particulate composites rather than syntactic foams and thus making the present study relevant. The major difference between solid particulate composite and syntactic foam lies in the void existing

Figure 1: Pictorial description of microballoon
within the microballoon. This void will also account for absorption of ultrasonic energy within the composite. Also, the interaction between particle and wave was not explicitly discussed in the earlier studies along with the effect of ratio of wavelength to particle size ratio on wave propagation in these composites and thus making the present study important.

In this study, a 2D transient pressure acoustics finite element model is developed to understand the effect of ratio of wavelength to particle size ratio on the wave interaction. Three different conditions for ratio of wavelength to particle size of equal to, greater than and lesser than 1 are considered.

2. Methods

This section describes the formulation of acoustic wave propagation through two-dimensional composite structures using COMSOL Acoustic Module. Emphasis is on modeling the effect of ratio of wavelength to particle size ratio on wave propagation. Three different conditions are examined: (i) ratio of wavelength to particle size greater than 1 (ii) ratio of wavelength to particle size lesser than 1, and (iii) ratio of wavelength to particle size equal to 1.

2.1 General Setup of the Acoustic Scattering Model

The computational domain is a square of side 25.4 mm filled with epoxy. Four microballoons (concentric circles with 90% void at the center) are located at four corners of the square with different acoustic properties (speed of sound, density, etc.) than those of the surrounding fluid. Material properties of epoxy and glass microballoon are as follows:

**Epoxy:**
Density = 1060 kg/m$^3$
Ultrasound velocity ($C_L$) (longitudinal wave) = 2838 m/s

**Glass Microballoon:**
Density = 220 kg/m$^3$
Ultrasound velocity ($C_L$) (longitudinal wave) = 1540 m/s

Wavelength of the wave ($\lambda_L$) = $C_L$/1MHz = 2.838 mm

The incident ultrasonic wave is modeled as a line source of 6.35 mm in length at the center of top horizontal line. A 1MHz frequency signal is applied through the line source for a time period of 1 µs. The input pressure signal is provided as a sine pulse with amplitude of 100 Pa.

$$P = A\sin(\omega t)$$  \hspace{1cm} (1)

Propagation of sound waves in the domain is described by the Helmholtz wave equation:

$$\nabla \cdot \left( \frac{-1}{\rho} \nabla p - q \right) = \frac{\partial^2 p}{\partial t^2} = Q$$  \hspace{1cm} (2)

where, $p$ is the acoustic pressure (Pa), $\rho$ is the density of epoxy surrounding the glass microballoon (Kg/m$^3$), $\omega$ is the angular frequency ($\omega = 2\Pi f$) of incident wave (s$^{-1}$), and $c$ is the longitudinal speed of sound (m/s).

Remaining part of the top horizontal line of the square is described by impedance of air by the following equation:

$$-n\left( \frac{-1}{\rho} \nabla p_i - q \right) = \frac{1}{z_i} \frac{\partial p_i}{\partial t}$$  \hspace{1cm} (3)

Other three sides of the square are considered as sound hard boundary and are described by the following equation:

$$-n\left( \frac{-1}{\rho} \nabla p_i - q \right) = 0$$  \hspace{1cm} (4)

Interface between epoxy and glass particle is considered as free boundary and the reflections at the interface are governed by the acoustic properties of epoxy and glass. Void is considered as interior sound hard boundary wall and is described by the following equation:

$$-n\left( \frac{-1}{\rho} \nabla p_i - q \right) = 0$$  \hspace{1cm} (5)

$$-n\left( \frac{-1}{\rho} \nabla p_i - q \right) = 0$$  \hspace{1cm} (6)

2.2 Meshing and Critical Time Step

The mesh is generated automatically with the triangular elements. Free meshing provided in COMSOL is used for the generation of mesh. Maximum and minimum element size for all the models is fixed at $\Delta x = 0.285$ mm corresponding approximately to $\lambda_L/10$. As per CFL criteria, the critical time steps to be used for simulation on FEM model for a time dependent solver is $\Delta x / C_L$ which is 0.285mm/2838m/s=1e-7. The time step for transient problem should be less than the
critical time step. Hence, in this study a time step of $5 \times 10^{-9}$ is selected in this study.

3. Results and Discussion

3.1 Case No: 1 Wavelength to particle size ratio greater than 1

In this study, hollow glass microballoon is modeled as two concentric circles with 0.6 mm and 0.54 mm diameter, respectively. Therefore, the wavelength to particle size ratio for this condition is 4.73, i.e., greater than 1. Meshing is performed using 24507 triangular elements and minimum element quality is 0.7941.

Figure 2 shows the geometry considered for this case. Pressure pulse as line source of sine wave applied at the center of the top horizontal line is shown in Figure 3. As the pressure pulse is modeled as a sine pulse of frequency 1 MHz and a time period of 1 µs, a positive pressure of 100 Pa was completed at $t=2.49 \times 10^{-7}$ sec as shown in Figure 4. After 1 µs, pressure ceases and as shown in Figure 5, envelope of both positive and negative pressure exist at $t=1\mu s$. The propagating wave front will diffuse through the thickness into spherical wave front.

Figure 2: Geometry for wavelength to particle size ratio greater than 1

Initial pressure pulse and pulse at a distance of 1.5 mm from the line source are as shown in Figure 6. Figure 7 shows the zoomed view of initial pulse at line source and at a distance of 1.5 mm. For the pulse to reach 1.5 mm, the time taken should be $1.5 \text{mm}/2838 \text{m/s}$ which is equal to $5.28 \times 10^{-7}$ sec. As shown in Figure 7, the pulse reached 1.5 mm point at approximately $5.2 \times 10^{-7}$ sec. Figure 8 shows the interaction of particle with the propagating wave front. From Figure 8 it can be also observed that the pressure at the center of microballoon, i.e., void is zero. It is also observed that the pressure in the glass particle is approximately 55 Pa. Figure 9 shows the pressure distribution at points inside the void, in the glass particle and at a point adjacent to particle. From Figure 9, it can be observed that the pressure in the void is zero. However, the pressure in the glass particle is observed to be more than the pressure at a point adjacent to particle. As the glass particle’s acoustic properties are lower compared to that of epoxy, it is expected that the reflection from the epoxy glass particle will be more and thus the pressure distribution within the glass particle should be lower than the epoxy. However, interface of glass particle and void is modeled as interior sound hard boundary wall. Due to this reason, the wave front propagating within glass particle interacts with interior sound hard boundary and thus increases the pressure in the glass particle.

Figure 3: Model showing pressure line source

Figure 4: Pressure distribution within composite at $t=2.49 \times 10^{-7}$. At this time pressure has reached 100 Pa
Figure 5: Pressure distribution showing positive and negative pulses of the sinewave

Figure 6: Waveforms showing pressure at line source and at a distance of 1.5 mm from the source

Figure 7: Zoomed view of initial pressure pulse at line source and at a distance of 1.5 mm from the source. Time delay in the pressure pulse at 1.5 mm distance from line source can be observed.

Figure 8: Pressure distribution surrounding glass microballoon. State of zero pressure within void can be observed.

Figure 9: Pressure distribution at the center of void, in the glass microballoon and point adjacent to glass microballoon.

3.2 Case No.2: Ratio of wavelength to particle size equal to 1.
In this study, hollow glass microballoon is modeled as two concentric circles with 2.8 mm and 2.52 mm diameter, respectively. Therefore, the wavelength to particle size ratio for this condition is 1. Meshing is performed using 22826 triangular elements with a minimum element quality of 0.8405. Figure 10 shows the geometry of the model used for this condition. Interaction of the wave and particle is as shown in Figure 11. Wave front splitting at the interface is observed in Figure 11. This behavior was not observed in Case 1. From Figure 12, it can be observed that the wave front was unable to cover the glass particle as in Case 1. Also, the maximum pressure within the glass particle is about 10 Pa. This is due to the reason that, at wavelength to particle size of 1, wave cannot
encompass the whole particle due to reflections and thus the pressure observed in the particle will be low. Figure 13 shows the pressure waveforms at points inside the void, in the glass particle and at a point adjacent to particle. From Figure 13, it can be observed that the pressure in the void is zero, whereas the pressure at the point adjacent to the particle is more compared to the point in the glass particle due to the increase in reflections from the particle surface.

Figure 10: Geometry of model for wavelength to particle size ratio equal to 1

Figure 11: Wave splitting at the glass microballoon surface.

Figure 12: Pressure distribution within the microballoon

Figure 13: Pressure distribution within the void, in glass and at a point adjacent to particle

3.3 Case No.3: Ratio of wavelength to particle size lesser than 1.

In this study, hollow glass microballoon is modeled as two concentric circles with 4mm and 3.6 mm diameter, respectively. Therefore, the wavelength to particle size ratio for this condition is 0.70, i.e., lesser than 1. Meshing is performed using 33481 triangular elements. Figure 14 shows the geometry of the model. Interaction of the wave with particle is shown in Figures 15 and 16. Unlike in Case 1 and 2, it could be observed that the wave bends at the particle interface. Also, the pressure in the glass particle is approximately 5 Pa. Points selected for observing the pressure distribution within void, glass particle and at point adjacent to glass particle are as shown in Figure 17. Pressure distribution at these three points are shown in Figure 18. Similar to Case 2, from Figure 18, it could be observed that the pressure in point adjacent to particle is more than the pressure in
glass particle. This is also due to the increased reflections from the surface. Trends observed in numerical studies cannot be experimentally validated as the volume fraction of particles is less than 1%. Hence, further studies have to be performed to validate these results experimentally.

4. Conclusions

Effect of wavelength to particle size ratio on wave propagation in syntactic foams is studied. Three different cases of wavelength to particle size ratios of greater than, lesser than and equal to 1 are considered. Sinusoidal pressure pulse is applied at center of the top horizontal line. Triangular elements with minimum and maximum size of 0.285 corresponding to λ/10 are used in this study. A critical time step of 5 ns is used for solving the transient pressure acoustics problem. For cases of wavelength to particle size ratio greater than 1, higher pressure distribution is observed within the glass particle compared to a point adjacent to the particle. Inner void is modeled as internal sound hard boundary wall. Due to this reason, waves interacting with the void boundary are reflected back completely. Also, pressure waves are found to encompass the whole glass particle with no pressure waves in the void. For cases of
wavelength to particle size ratio of equal to 1 and lesser than 1, it is observed that the pressure distribution within the glass particle is lower compared to the point adjacent to glass particle.

5. References

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